

SADLIER

## Progress in Mathematics

SADLIER

## Common Core Progress Mathematics

## Common Core State Standards for Mathematics

# Grade 3 Crosswalk

Skills Update—Review of Grade 2 Skills	2
1. Place Value	4
2. Addition	5
3. Subtraction	7
4. Multiplication Concepts and Facts	10
5. Division Concepts and Facts	14
6. More Multiplication and Division Facts	17
7. Statistics and Probability	25
8. Measurement and Time	27
9. Geometry	29
10. Multiply by One Digit	33
11. Divide by One Digit	35
12. Fractions	35
13. Decimals	40
14. More Concepts in Algebra	40

## Skills Update—Review of Grade 2 Skills

PROGRESS IN MATHEMATICS, GRADE 3	COMMON CORE PROGRESS MATHEMATICS, GRADE 3	COMMON CORE STATE STANDARDS FOR MATHEMATICS, GRADE 3
SU <b>Expanded Form</b> —p. 1		
SU <b>Count by 2s, 5s, 10s</b> —p. 2		
SU <b>Money Less Than \$1.00</b> —p. 3		
SU <b>Addition Facts Through 18</b> —p. 4	<b>Lesson 14   Add and Subtract Fluently within 1000</b> —pp. 120–127	3.NBT.2    Fluently add and subtract within 1000 using strategies and algorithms based on place value, properties of operations, and/or the relationship between addition and subtraction.
SU <b>Subtraction Facts Through 18</b> —p. 5		
SU <b>Mental Math Strategies</b> —p. 6		
SU <b>Patterns</b> —p. 7	<b>Lesson 12   Identify and Explain Arithmetic Patterns</b> —pp. 104–111	3.OA.9    Identify arithmetic patterns (including patterns in the addition table or multiplication table), and explain them using properties of operations.  <i>For example, observe that 4 times a number is always even, and explain why 4 times a number can be decomposed into two equal addends.</i>
SU <b>Fractions: Part of a Whole</b> —p. 8	<b>Lesson 16   Understand Unit Fractions as Quantities</b> —pp. 142–149	3.NF.1    Understand a fraction $1/b$ as the quantity formed by 1 part when a whole is partitioned into $b$ equal parts; understand a fraction $a/b$ as the quantity formed by $a$ parts of size $1/b$ .
SU <b>Fractions: Part of a Set</b> —p. 9	<b>Lesson 17   Understand Fractions as Quantities</b> —pp. 150–157	3.G.2    Partition shapes into parts with equal areas. Express the area of each part as a unit fraction of the whole.  <i>For example, partition a shape into 4 parts with equal area, and describe the area of each part as <math>1/4</math> of the area of the shape.</i>
SU <b>Nonstandard Units</b> —p. 10	<b>Lesson 36   Partition Shapes to Make Equal Areas</b> —pp. 320–327	
SU <b>Inch and Centimeter</b> —p. 11		

### Skills Update—Review of Grade 2 Skills

**PROGRESS IN MATHEMATICS, GRADE 3**

<b>SU</b>	<b>Cup, Pint, Quart</b> —p. 12
<b>SU</b>	<b>Liter</b> —p. 13
<hr/>	
<b>SU</b>	<b>Hour, Half Hour</b> —p. 14
<hr/>	
<b>SU</b>	<b>A.M., P.M.</b> —p. 15
<b>SU</b>	<b>Sides and Vertices</b> —p. 16
<b>SU</b>	<b>Solid Figures</b> —p. 17
<b>SU</b>	<b>Venn Diagrams</b> —p. 18
<b>SU</b>	<b>Read a Pictograph</b> —p. 19
<b>SU</b>	<b>Read a Bar Graph</b> —p. 20
<b>SU</b>	<b>Certain, Possible, Impossible Outcomes</b> —p. 21

**COMMON CORE PROGRESS MATHEMATICS, GRADE 3**

<b>Lesson 25</b>	<b>Problem Solving: Volumes and Masses</b> —pp. 226–233
<b>Lesson 32</b>	<b>Problem Solving: Measurement</b> —pp. 288–295
<hr/>	
<b>Lesson 24</b>	<b>Problem Solving: Time</b> —pp. 218–225
<hr/>	

**COMMON CORE STATE STANDARDS FOR MATHEMATICS, GRADE 3**

<b>3.MD.2</b>	<p>Measure and estimate liquid volumes and masses of objects using standard units of grams (g), kilograms (kg), and liters (l).<sup>6</sup> Add, subtract, multiply, or divide to solve one-step word problems involving masses or volumes that are given in the same units, e.g., by using drawings (such as a beaker with a measurement scale) to represent the problem.<sup>7</sup></p> <p><sup>6</sup>Excludes compound units such as cm<sup>3</sup> and finding the geometric volume of a container.</p> <p><sup>7</sup>Excludes multiplicative comparison problems (problems involving notions of “times as much.”)</p>
<b>3.MD.1</b>	<p>Tell and write time to the nearest minute and measure time intervals in minutes. Solve word problems involving addition and subtraction of time intervals in minutes, e.g., by representing the problem on a number line diagram.</p>

**Chapter 1 Place Value**

PROGRESS IN MATHEMATICS, GRADE 3	
1-1	<b>Hundreds</b> —pp. 30–31
1-2	<b>Compare Numbers</b> —pp. 32–33
1-3	<b>Order Numbers</b> —pp. 34–35
1-4	<b>Counting Patterns</b> —pp. 36–37
1-5	<b>What Is One Thousand?</b> —pp. 38–39
1-6	<b>Thousands</b> —pp. 40–41
1-7	<b>Ten Thousands and Hundred Thousands</b> —pp. 42–43
1-8	<b>Compare and Order Larger Numbers</b> —pp. 44–45
1-9	<b>Round Numbers</b> —pp. 46–47
1-10	<b>Coins and Bills</b> —pp. 48–49
1-11	<b>Make and Count Change</b> —pp. 50–51
1-12	<b>Compare and Round Money</b> —pp. 52–53
1-13	<b>Problem Solving Strategy: Draw a Picture</b> —pp. 54–55
1-14	<b>Problem Solving Applications: Mixed Review</b> —pp. 56–57

COMMON CORE PROGRESS MATHEMATICS, GRADE 3	
<b>Lesson 12</b>	<b>Identify and Explain Arithmetic Patterns</b> —pp. 104–111
<b>Lesson 13</b>	<b>Round Whole Numbers to the Nearest 10 or 100</b> —pp. 112–119

COMMON CORE STATE STANDARDS FOR MATHEMATICS, GRADE 3	
3.OA.9	Identify arithmetic patterns (including patterns in the addition table or multiplication table), and explain them using properties of operations.  <i>For example, observe that 4 times a number is always even, and explain why 4 times a number can be decomposed into two equal addends.</i>
3.NBT.1	Use place value understanding to round whole numbers to the nearest 10 or 100.

## Chapter 2 Addition

PROGRESS IN MATHEMATICS, GRADE 3	COMMON CORE PROGRESS MATHEMATICS, GRADE 3	COMMON CORE STATE STANDARDS FOR MATHEMATICS, GRADE 3
<b>2-1</b> <b>More Than Two Addends</b> —pp. 64–65		
<b>2-2</b> <b>Missing Addends</b> —pp. 66–67	<b>Lesson 10</b> <b>Problem Solving: Two-Step Problems</b> —pp. 88–95	3.OA.8    Solve two-step word problems using the four operations. Represent these problems using equations with a letter standing for the unknown quantity. Assess the reasonableness of answers using mental computation and estimation strategies including rounding. <sup>3</sup>
	<b>Lesson 11</b> <b>Problem Solving: Use Equations</b> —pp. 96–103	<sup>3</sup> This standard is limited to problems posed with whole numbers and having whole-number answers; students should know how to perform operations in the conventional order when there are no parentheses to specify a particular order (Order of Operations).
<b>2-3</b> <b>Add No Regrouping</b> —pp. 68–69	<b>Lesson 14</b> <b>Add and Subtract Fluently within 1000</b> —pp. 120–127	3.NBT.2    Fluently add and subtract within 1000 using strategies and algorithms based on place value, properties of operations, and/or the relationship between addition and subtraction.
<b>2-4</b> <b>Estimate Sums</b> —pp. 70–71	<b>Lesson 13</b> <b>Round Whole Numbers to the Nearest 10 or 100</b> —pp. 112–119	3.NBT.1    Use place value understanding to round whole numbers to the nearest 10 or 100.
<b>2-5</b> <b>Add with Regrouping</b> —pp. 72–73	<b>Lesson 13</b> <b>Round Whole Numbers to the Nearest 10 or 100</b> —pp. 112–119	3.NBT.1    Use place value understanding to round whole numbers to the nearest 10 or 100.
	<b>Lesson 14</b> <b>Add and Subtract Fluently within 1000</b> —pp. 120–127	3.NBT.2    Fluently add and subtract within 1000 using strategies and algorithms based on place value, properties of operations, and/or the relationship between addition and subtraction.
<b>2-6</b> <b>Regroup Tens</b> —p. 74	<b>Lesson 14</b> <b>Add and Subtract Fluently within 1000</b> —pp. 120–127	3.NBT.2    Fluently add and subtract within 1000 using strategies and algorithms based on place value, properties of operations, and/or the relationship between addition and subtraction.
<b>2-7</b> <b>Add Regroup Tens</b> —p. 75	<b>Lesson 13</b> <b>Round Whole Numbers to the Nearest 10 or 100</b> —pp. 112–119	3.NBT.1    Use place value understanding to round whole numbers to the nearest 10 or 100.
<b>2-8</b> <b>Add Regroup Twice</b> —pp. 76–77	<b>Lesson 14</b> <b>Add and Subtract Fluently within 1000</b> —pp. 120–127	3.NBT.2    Fluently add and subtract within 1000 using strategies and algorithms based on place value, properties of operations, and/or the relationship between addition and subtraction.

## Chapter 2 Addition

PROGRESS IN MATHEMATICS, GRADE 3	COMMON CORE PROGRESS MATHEMATICS, GRADE 3	COMMON CORE STATE STANDARDS FOR MATHEMATICS, GRADE 3
<b>*2-8A Addition Properties</b> —Online	<b>Lesson 14 Add and Subtract Fluently within 1000</b> —pp. 120–127	3.NBT.2 Fluently add and subtract within 1000 using strategies and algorithms based on place value, properties of operations, and/or the relationship between addition and subtraction.
<b>2-9 Three-Digit Addition</b> —pp. 78–79	<b>Lesson 13 Round Whole Numbers to the Nearest 10 or 100</b> —pp. 112–119	3.NBT.1 Use place value understanding to round whole numbers to the nearest 10 or 100.
<b>2-10 More Regrouping in Addition</b> —pp. 80–81	<b>Lesson 14 Add and Subtract Fluently within 1000</b> —pp. 120–127	3.NBT.2 Fluently add and subtract within 1000 using strategies and algorithms based on place value, properties of operations, and/or the relationship between addition and subtraction.
<b>2-11 Mental Math</b> —pp. 82–83	<b>Lesson 14 Add and Subtract Fluently within 1000</b> —pp. 120–127	3.NBT.2 Fluently add and subtract within 1000 using strategies and algorithms based on place value, properties of operations, and/or the relationship between addition and subtraction.
<b>2-12 Regroup Hundreds as Thousands</b> —pp. 84–85	<b>Lesson 14 Add and Subtract Fluently within 1000</b> —pp. 120–127	3.NBT.2 Fluently add and subtract within 1000 using strategies and algorithms based on place value, properties of operations, and/or the relationship between addition and subtraction.
<b>2-13 Three or More Addends</b> —pp. 86–87	<b>Lesson 13 Round Whole Numbers to the Nearest 10 or 100</b> —pp. 112–119	3.NBT.1 Use place value understanding to round whole numbers to the nearest 10 or 100.
<b>2-14 Add Larger Numbers</b> —pp. 88–89	<b>Lesson 10 Problem Solving: Two-Step Problems</b> —pp. 88–95	3.OA.8 Solve two-step word problems using the four operations. Represent these problems using equations with a letter standing for the unknown quantity. Assess the reasonableness of answers using mental computation and estimation strategies including rounding. <sup>3</sup>
<b>2-15 Problem Solving Strategy: Use Simpler Numbers</b> —pp. 90–91	<b>Lesson 11 Problem Solving: Use Equations</b> —pp. 96–103	<sup>3</sup> This standard is limited to problems posed with whole numbers and having whole-number answers; students should know how to perform operations in the conventional order when there are no parentheses to specify a particular order (Order of Operations).
<b>2-16 Problem Solving Applications: Mixed Review</b> —pp. 92–93	<b>Lesson 13 Round Whole Numbers to the Nearest 10 or 100</b> —pp. 112–119	3.NBT.1 Use place value understanding to round whole numbers to the nearest 10 or 100.
	<b>Lesson 10 Problem Solving: Two-Step Problems</b> —pp. 88–95	3.OA.8 Solve two-step word problems using the four operations. Represent these problems using equations with a letter standing for the
	<b>Lesson 11 Problem Solving: Use Equations</b> —pp. 96–103	– continued on next page –

## Chapter 2 Addition

PROGRESS IN MATHEMATICS, GRADE 3

COMMON CORE PROGRESS MATHEMATICS, GRADE 3

COMMON CORE STATE STANDARDS FOR MATHEMATICS, GRADE 3

*– continued from previous page –*

unknown quantity. Assess the reasonableness of answers using mental computation and estimation strategies including rounding.<sup>3</sup>

<sup>3</sup>This standard is limited to problems posed with whole numbers and having whole-number answers; students should know how to perform operations in the conventional order when there are no parentheses to specify a particular order (Order of Operations).

## Chapter 3 Subtraction

PROGRESS IN MATHEMATICS, GRADE 3

COMMON CORE PROGRESS MATHEMATICS, GRADE 3

COMMON CORE STATE STANDARDS FOR MATHEMATICS, GRADE 3

**3-1 Subtraction Concepts**—pp. 100–101

**3-2 Subtract: No Regrouping**—pp. 102–103

**3-3 Estimate Differences**—pp. 104–105

**3-4 Subtract with Regrouping**—pp. 106–107

**Lesson 10 Problem Solving: Two-Step Problems**—pp. 88–95

**Lesson 11 Problem Solving: Use Equations**—pp. 96–103

**Lesson 13 Round Whole Numbers to the Nearest 10 or 100**—pp. 112–119

**Lesson 14 Add and Subtract Fluently within 1000**—pp. 120–127

3.OA.8 Solve two-step word problems using the four operations. Represent these problems using equations with a letter standing for the unknown quantity. Assess the reasonableness of answers using mental computation and estimation strategies including rounding.<sup>3</sup>

<sup>3</sup>This standard is limited to problems posed with whole numbers and having whole-number answers; students should know how to perform operations in the conventional order when there are no parentheses to specify a particular order (Order of Operations).

3.NBT.1 Use place value understanding to round whole numbers to the nearest 10 or 100.

3.NBT.2 Fluently add and subtract within 1000 using strategies and algorithms based on place value, properties of operations, and/or the relationship between addition and subtraction.

## Chapter 3 Subtraction

PROGRESS IN MATHEMATICS, GRADE 3	COMMON CORE PROGRESS MATHEMATICS, GRADE 3	COMMON CORE STATE STANDARDS FOR MATHEMATICS, GRADE 3
3-5 <b>Regroup Hundreds and Dollars</b> —pp. 108–109	<b>Lesson 14 Add and Subtract Fluently within 1000</b> —pp. 120–127	3.NBT.2 Fluently add and subtract within 1000 using strategies and algorithms based on place value, properties of operations, and/or the relationship between addition and subtraction.
3-6 <b>Regroup Once in Subtraction</b> —pp. 110–111	<b>Lesson 13 Round Whole Numbers to the Nearest 10 or 100</b> —pp. 112–119 <b>Lesson 14 Add and Subtract Fluently within 1000</b> —pp. 120–127	3.NBT.1 Use place value understanding to round whole numbers to the nearest 10 or 100. 3.NBT.2 Fluently add and subtract within 1000 using strategies and algorithms based on place value, properties of operations, and/or the relationship between addition and subtraction.
3-7 <b>Regroup Twice in Subtraction</b> —pp. 112–113	<b>Lesson 10 Problem Solving: Two-Step Problems</b> —pp. 88–95 <b>Lesson 11 Problem Solving: Use Equations</b> —pp. 96–103  <b>Lesson 13 Round Whole Numbers to the Nearest 10 or 100</b> —pp. 112–119 <b>Lesson 14 Add and Subtract Fluently within 1000</b> —pp. 120–127	3.OA.8 Solve two-step word problems using the four operations. Represent these problems using equations with a letter standing for the unknown quantity. Assess the reasonableness of answers using mental computation and estimation strategies including rounding. <sup>3</sup>  <sup>3</sup> This standard is limited to problems posed with whole numbers and having whole-number answers; students should know how to perform operations in the conventional order when there are no parentheses to specify a particular order (Order of Operations). 3.NBT.1 Use place value understanding to round whole numbers to the nearest 10 or 100. 3.NBT.2 Fluently add and subtract within 1000 using strategies and algorithms based on place value, properties of operations, and/or the relationship between addition and subtraction.
3-8 <b>Regroup with Zeros</b> —pp. 114–115	<b>Lesson 13 Round Whole Numbers to the Nearest 10 or 100</b> —pp. 112–119 <b>Lesson 14 Add and Subtract Fluently within 1000</b> —pp. 120–127	3.NBT.1 Use place value understanding to round whole numbers to the nearest 10 or 100. 3.NBT.2 Fluently add and subtract within 1000 using strategies and algorithms based on place value, properties of operations, and/or the relationship between addition and subtraction.

**Chapter 3 Subtraction**

PROGRESS IN MATHEMATICS, GRADE 3	
<b>3-9</b>	<b>Regroup Thousands as Hundreds</b> —pp. 116–117
<b>3-10</b>	<b>Subtract Larger Numbers</b> —pp. 118–119
<b>3-11</b>	<b>Choose a Computation Method</b> —pp. 120–121
<b>3-12</b>	<b>Problem Solving Strategy: Choose the Operation</b> —pp. 122–123
<b>*3-12A</b>	<b>Missing Operands</b> —Online
<b>3-13</b>	<b>Problem Solving Applications: Mixed Review</b> —pp. 124–125

COMMON CORE PROGRESS MATHEMATICS, GRADE 3	
<b>Lesson 13</b>	<b>Round Whole Numbers to the Nearest 10 or 100</b> —pp. 112–119
<b>Lesson 10</b>	<b>Problem Solving: Two-Step Problems</b> —pp. 88–95
<b>Lesson 11</b>	<b>Problem Solving: Use Equations</b> —pp. 96–103
<b>Lesson 13</b>	<b>Round Whole Numbers to the Nearest 10 or 100</b> —pp. 112–119
<b>Lesson 14</b>	<b>Add and Subtract Fluently within 1000</b> —pp. 120–127
<b>Lesson 10</b>	<b>Problem Solving: Two-Step Problems</b> —pp. 88–95
<b>Lesson 11</b>	<b>Problem Solving: Use Equations</b> —pp. 96–103

COMMON CORE STATE STANDARDS FOR MATHEMATICS, GRADE 3	
3.NBT.1	Use place value understanding to round whole numbers to the nearest 10 or 100.
3.OA.8	Solve two-step word problems using the four operations. Represent these problems using equations with a letter standing for the unknown quantity. Assess the reasonableness of answers using mental computation and estimation strategies including rounding. <sup>3</sup>  <sup>3</sup> This standard is limited to problems posed with whole numbers and having whole-number answers; students should know how to perform operations in the conventional order when there are no parentheses to specify a particular order (Order of Operations).
3.NBT.1	Use place value understanding to round whole numbers to the nearest 10 or 100.
3.NBT.2	Fluently add and subtract within 1000 using strategies and algorithms based on place value, properties of operations, and/or the relationship between addition and subtraction.
3.OA.8	Solve two-step word problems using the four operations. Represent these problems using equations with a letter standing for the unknown quantity. Assess the reasonableness of answers using mental computation and estimation strategies including rounding. <sup>3</sup>  <sup>3</sup> This standard is limited to problems posed with whole numbers and having whole-number answers; students should know how to perform operations in the conventional order when there are no parentheses to specify a particular order (Order of Operations).

**Chapter 4 Multiplication Concepts and Facts**

PROGRESS IN MATHEMATICS, GRADE 3	
<b>4-1</b>	<b>Understand Multiplication</b> —pp. 132–133
<b>4-2</b>	<b>One and Zero as Factors</b> —pp. 134–135
<b>4-3</b>	<b>Multiply Twos</b> —pp. 136–137
<b>4-4</b>	<b>Multiply Threes</b> —pp. 138–139
<b>4-5</b>	<b>Multiply Fours</b> —pp. 140–141
<b>4-6</b>	<b>Multiply Fives</b> —pp. 142–143

COMMON CORE PROGRESS MATHEMATICS, GRADE 3	
<b>Lesson 1</b>	<b>Interpret Products of Whole Numbers</b> —pp. 10–17
<b>Lesson 1</b>	<b>Interpret Products of Whole Numbers</b> —pp. 10–17
<b>Lesson 6</b>	<b>Apply Commutative and Associative Properties to Multiply</b> —pp. 50–57
<b>Lesson 7</b>	<b>Apply the Distributive Property to Multiply</b> —pp. 58–65
<b>Lesson 1</b>	<b>Interpret Products of Whole Numbers</b> —pp. 10–17
<b>Lesson 3</b>	<b>Problem Solving: Multiplication/Division and Equal Groups</b> —pp. 26–33
<b>Lesson 4</b>	<b>Problem Solving: Multiplication/Division and Arrays</b> —pp. 34–41
<b>Lesson 32</b>	<b>Problem Solving: Measurement</b> —pp. 288–295

COMMON CORE STATE STANDARDS FOR MATHEMATICS, GRADE 3	
3.OA.1	Interpret products of whole numbers, e.g., interpret $5 \times 7$ as the total number of objects in 5 groups of 7 objects each. <i>For example, describe a context in which a total number of objects can be expressed as <math>5 \times 7</math>.</i>
3.OA.1	Interpret products of whole numbers, e.g., interpret $5 \times 7$ as the total number of objects in 5 groups of 7 objects each. <i>For example, describe a context in which a total number of objects can be expressed as <math>5 \times 7</math>.</i>
3.OA.5	Apply properties of operations as strategies to multiply and divide. <sup>2</sup> <i>Examples: If <math>6 \times 4 = 24</math> is known, then <math>4 \times 6 = 24</math> is also known. (Commutative property of multiplication.) <math>3 \times 5 \times 2</math> can be found by <math>3 \times 5 = 15</math>, then <math>15 \times 2 = 30</math>, or by <math>5 \times 2 = 10</math>, then <math>3 \times 10 = 30</math>. (Associative property of multiplication.) Knowing that <math>8 \times 5 = 40</math> and <math>8 \times 2 = 16</math>, one can find <math>8 \times 7</math> as <math>8 \times (5 + 2) = (8 \times 5) + (8 \times 2) = 40 + 16 = 56</math>. (Distributive property.)</i> <sup>2</sup> Students need not use formal terms for these properties.
3.OA.1	Interpret products of whole numbers, e.g., interpret $5 \times 7$ as the total number of objects in 5 groups of 7 objects each. <i>For example, describe a context in which a total number of objects can be expressed as <math>5 \times 7</math>.</i>
3.OA.3	Use multiplication and division within 100 to solve word problems in situations involving equal groups, arrays, and measurement quantities, e.g., by using drawings and equations with a symbol for the unknown number to represent the problem.

## Chapter 4 Multiplication Concepts and Facts

PROGRESS IN MATHEMATICS, GRADE 3	COMMON CORE PROGRESS MATHEMATICS, GRADE 3	COMMON CORE STATE STANDARDS FOR MATHEMATICS, GRADE 3
<b>*4-6A</b> Multiplication and Arrays—Online	<b>Lesson 12</b> Identify and Explain Arithmetic Patterns—pp. 104–111	3.OA.9 Identify arithmetic patterns (including patterns in the addition table or multiplication table), and explain them using properties of operations.  <i>For example, observe that 4 times a number is always even, and explain why 4 times a number can be decomposed into two equal addends.</i>
<b>*4-6B</b> Use a Bar Diagram to Multiply—Online	<b>Lesson 1</b> Interpret Products of Whole Numbers—pp. 10–17	3.OA.1 Interpret products of whole numbers, e.g., interpret $5 \times 7$ as the total number of objects in 5 groups of 7 objects each.  <i>For example, describe a context in which a total number of objects can be expressed as <math>5 \times 7</math>.</i>
<b>*4-6C</b> Multiplication Stories—Online	<b>Lesson 3</b> Problem Solving: Multiplication/Division and Equal Groups—pp. 26–33	3.OA.3 Use multiplication and division within 100 to solve word problems in situations involving equal groups, arrays, and measurement quantities, e.g., by using drawings and equations with a symbol for the unknown number to represent the problem.
	<b>Lesson 4</b> Problem Solving: Multiplication/Division and Arrays—pp. 34–41	3.OA.3 Use multiplication and division within 100 to solve word problems in situations involving equal groups, arrays, and measurement quantities, e.g., by using drawings and equations with a symbol for the unknown number to represent the problem.
	<b>Lesson 32</b> Problem Solving: Measurement—pp. 288–295	3.OA.8 Solve two-step word problems using the four operations. Represent these problems using equations with a letter standing for the unknown quantity. Assess the reasonableness of answers using mental computation and estimation strategies including rounding. <sup>3</sup>
	<b>Lesson 3</b> Problem Solving: Multiplication/Division and Equal Groups—pp. 26–33	<sup>3</sup> This standard is limited to problems posed with whole numbers and having whole-number answers;
	<b>Lesson 4</b> Problem Solving: Multiplication/Division and Arrays—pp. 34–41	– continued on next page –
	<b>Lesson 32</b> Problem Solving: Measurement—pp. 288–295	
	<b>Lesson 10</b> Problem Solving: Two-Step Problems—pp. 88–95	
	<b>Lesson 11</b> Problem Solving: Use Equations—pp. 96–103	

**Chapter 4 Multiplication Concepts and Facts**

PROGRESS IN MATHEMATICS, GRADE 3

COMMON CORE PROGRESS MATHEMATICS, GRADE 3

COMMON CORE STATE STANDARDS FOR MATHEMATICS, GRADE 3

– continued from previous page –

students should know how to perform operations in the conventional order when there are no parentheses to specify a particular order (Order of Operations).

**4-7 Multiply Cents**—pp. 144–145

**Lesson 1 Interpret Products of Whole Numbers**—pp. 10–17

3.OA.1 Interpret products of whole numbers, e.g., interpret  $5 \times 7$  as the total number of objects in 5 groups of 7 objects each.

*For example, describe a context in which a total number of objects can be expressed as  $5 \times 7$ .*

**Lesson 3 Problem Solving: Multiplication/Division and Equal Groups**—pp. 26–33

3.OA.3 Use multiplication and division within 100 to solve word problems in situations involving equal groups, arrays, and measurement quantities, e.g., by using drawings and equations with a symbol for the unknown number to represent the problem.

**Lesson 4 Problem Solving: Multiplication/Division and Arrays**—pp. 34–41

**Lesson 32 Problem Solving: Measurement**—pp. 288–295

**4-8 Sums, Differences, and Products**—pp. 146–147

**Lesson 10 Problem Solving: Two-Step Problems**—pp. 88–95

3.OA.8 Solve two-step word problems using the four operations. Represent these problems using equations with a letter standing for the unknown quantity. Assess the reasonableness of answers using mental computation and estimation strategies including rounding.<sup>3</sup>

<sup>3</sup>This standard is limited to problems posed with whole numbers and having whole-number answers; students should know how to perform operations in the conventional order when there are no parentheses to specify a particular order (Order of Operations).

**Lesson 11 Problem Solving: Use Equations**—pp. 96–103

**4-9 Order in Multiplication**—pp. 148–149

**Lesson 6 Apply Commutative and Associative Properties to Multiply**—pp. 50–57

3.OA.5 Apply properties of operations as strategies to multiply and divide.<sup>2</sup>

*Examples: If  $6 \times 4 = 24$  is known, then  $4 \times 6 = 24$  is also known. (Commutative property of multiplication.)  $3 \times 5 \times 2$  can be found by  $3 \times 5 = 15$ , then  $15 \times 2 = 30$ , or by  $5 \times 2 = 10$ , then  $3 \times 10 =$*

– continued on next page –

## Chapter 4 Multiplication Concepts and Facts

PROGRESS IN MATHEMATICS, GRADE 3	COMMON CORE PROGRESS MATHEMATICS, GRADE 3	COMMON CORE STATE STANDARDS FOR MATHEMATICS, GRADE 3
		<p>– continued from previous page –</p> <p>30. (Associative property of multiplication.) Knowing that <math>8 \times 5 = 40</math> and <math>8 \times 2 = 16</math>, one can find <math>8 \times 7</math> as <math>8 \times (5 + 2) = (8 \times 5) + (8 \times 2) = 40 + 16 = 56</math>. (Distributive property.)</p> <p><sup>2</sup>Students need not use formal terms for these properties.</p>
<p><b>4-10 Missing Factors</b>—pp. 150–151</p>	<p><b>Lesson 5 Find Unknown Numbers in Multiplication and Division Equations</b>—pp. 42–49</p>	<p>3.OA.4 Determine the unknown whole number in a multiplication or division equation relating three whole numbers.</p> <p><i>For example, determine the unknown number that makes the equation true in each of the equations <math>8 \times ? = 48</math>, <math>5 = \square \div 3</math>, <math>6 \times 6 = ?</math>.</i></p>
	<p><b>Lesson 8 Divide by Finding an Unknown Factor</b>—pp. 66–73</p>	<p>3.OA.6 Understand division as an unknown-factor problem.</p> <p><i>For example, find <math>32 \div 8</math> by finding the number that makes 32 when multiplied by 8. Multiply and divide within 100.</i></p>
<p><b>4-11 Problem Solving Strategy: Use More Than One Step</b>—pp. 152–153</p>	<p><b>Lesson 10 Problem Solving: Two-Step Problems</b>—pp. 88–95</p>	<p>3.OA.8 Solve two-step word problems using the four operations. Represent these problems using equations with a letter standing for the unknown quantity. Assess the reasonableness of answers using mental computation and estimation strategies including rounding.<sup>3</sup></p> <p><sup>3</sup>This standard is limited to problems posed with whole numbers and having whole-number answers; students should know how to perform operations in the conventional order when there are no parentheses to specify a particular order (Order of Operations).</p>

**Chapter 4 Multiplication Concepts and Facts**

PROGRESS IN MATHEMATICS, GRADE 3

**4-12 Problem Solving Applications: Mixed Review**—pp. 154–155

COMMON CORE PROGRESS MATHEMATICS, GRADE 3

**Lesson 3 Problem Solving: Multiplication/Division and Equal Groups**—pp. 26–33

**Lesson 4 Problem Solving: Multiplication/Division and Arrays**—pp. 34–41

**Lesson 32 Problem Solving: Measurement**—pp. 288–295

COMMON CORE STATE STANDARDS FOR MATHEMATICS, GRADE 3

3.OA.3 Use multiplication and division within 100 to solve word problems in situations involving equal groups, arrays, and measurement quantities, e.g., by using drawings and equations with a symbol for the unknown number to represent the problem.

**Chapter 5 Division Concepts and Facts**

PROGRESS IN MATHEMATICS, GRADE 3

**5-1 Understand Division**—pp. 162–163

COMMON CORE PROGRESS MATHEMATICS, GRADE 3

**Lesson 2 Interpret Quotients of Whole Numbers**—pp. 18–26

**Lesson 3 Problem Solving: Multiplication/Division and Equal Groups**—pp. 26–33

**Lesson 4 Problem Solving: Multiplication/Division and Arrays**—pp. 34–41

**Lesson 32 Problem Solving: Measurement**—pp. 288–295

COMMON CORE STATE STANDARDS FOR MATHEMATICS, GRADE 3

3.OA.2 Interpret whole-number quotients of whole numbers, e.g., interpret  $56 \div 8$  as the number of objects in each share when 56 objects are partitioned equally into 8 shares, or as a number of shares when 56 objects are partitioned into equal shares of 8 objects each.

*For example, describe a context in which a number of shares or a number of groups can be expressed as  $56 \div 8$ .*

3.OA.3 Use multiplication and division within 100 to solve word problems in situations involving equal groups, arrays, and measurement quantities, e.g., by using drawings and equations with a symbol for the unknown number to represent the problem.

**5-2 One and Zero in Division**—pp. 164–165

**Lesson 2 Interpret Quotients of Whole Numbers**—pp. 18–26

3.OA.2 Interpret whole-number quotients of whole numbers, e.g., interpret  $56 \div 8$  as the number of objects in each share when 56 objects are partitioned equally into 8 shares, or as a number of shares when 56 objects are partitioned into equal shares of 8 objects each.

– continued on next page –

**Chapter 5 Division Concepts and Facts**

PROGRESS IN MATHEMATICS, GRADE 3

- 5-3**    **Divide by 2**—pp. 166–167
- 5-4**    **Divide by 3**—pp. 168–169
- 5-5**    **Divide by 4**—pp. 170–171
- 5-6**    **Divide by 5**—pp. 172–173

**\*5-6A**    **Division Stories**—Online

COMMON CORE PROGRESS MATHEMATICS, GRADE 3

**Lesson 2**    **Interpret Quotients of Whole Numbers**—pp. 18–26

**Lesson 3**    **Problem Solving: Multiplication/Division and Equal Groups**—pp. 26–33

**Lesson 4**    **Problem Solving: Multiplication/Division and Arrays**—pp. 34–41

**Lesson 32**    **Problem Solving: Measurement**—pp. 288–295

**Lesson 12**    **Identify and Explain Arithmetic Patterns**—pp. 104–111

**Lesson 2**    **Interpret Quotients of Whole Numbers**—pp. 18–26

COMMON CORE STATE STANDARDS FOR MATHEMATICS, GRADE 3

– continued from previous page –

*For example, describe a context in which a number of shares or a number of groups can be expressed as  $56 \div 8$ .*

3.OA.2    Interpret whole-number quotients of whole numbers, e.g., interpret  $56 \div 8$  as the number of objects in each share when 56 objects are partitioned equally into 8 shares, or as a number of shares when 56 objects are partitioned into equal shares of 8 objects each.

*For example, describe a context in which a number of shares or a number of groups can be expressed as  $56 \div 8$ .*

3.OA.3    Use multiplication and division within 100 to solve word problems in situations involving equal groups, arrays, and measurement quantities, e.g., by using drawings and equations with a symbol for the unknown number to represent the problem.

3.OA.9    Identify arithmetic patterns (including patterns in the addition table or multiplication table), and explain them using properties of operations.

*For example, observe that 4 times a number is always even, and explain why 4 times a number can be decomposed into two equal addends.*

3.OA.2    Interpret whole-number quotients of whole numbers, e.g., interpret  $56 \div 8$  as the number of objects in each share when 56 objects are partitioned equally into 8 shares, or as a number of shares when 56 objects are

– continued on next page –

## Chapter 5 Division Concepts and Facts

## PROGRESS IN MATHEMATICS, GRADE 3

**5-7** **Relate Multiplication and Division**—pp. 174–175

**5-8** **Divide Cents**—pp. 176–177

## COMMON CORE PROGRESS MATHEMATICS, GRADE 3

**Lesson 3** **Problem Solving: Multiplication/Division and Equal Groups**—pp. 26–33

**Lesson 4** **Problem Solving: Multiplication/Division and Arrays**—pp. 34–41

**Lesson 32** **Problem Solving: Measurement**—pp. 288–295

**Lesson 8** **Divide by Finding an Unknown Factor**—pp. 66–73

**Lesson 9** **Multiply and Divide Fluently within 100**—pp. 80–87

**Lesson 2** **Interpret Quotients of Whole Numbers**—pp. 18–26

## COMMON CORE STATE STANDARDS FOR MATHEMATICS, GRADE 3

– continued from previous page –

partitioned into equal shares of 8 objects each.

*For example, describe a context in which a number of shares or a number of groups can be expressed as  $56 \div 8$ .*

**3.OA.3** Use multiplication and division within 100 to solve word problems in situations involving equal groups, arrays, and measurement quantities, e.g., by using drawings and equations with a symbol for the unknown number to represent the problem.

**3.OA.6** Understand division as an unknown-factor problem.

*For example, find  $32 \div 8$  by finding the number that makes 32 when multiplied by 8. Multiply and divide within 100.*

**3.OA.7** Fluently multiply and divide within 100, using strategies such as the relationship between multiplication and division (e.g., knowing that  $8 \times 5 = 40$ , one knows  $40 \div 5 = 8$ ) or properties of operations. By the end of Grade 3, know from memory all products of two one-digit numbers. Solve problems involving the four operations, and identify and explain patterns in arithmetic.

**3.OA.2** Interpret whole-number quotients of whole numbers, e.g., interpret  $56 \div 8$  as the number of objects in each share when 56 objects are partitioned equally into 8 shares, or as a number of shares when 56 objects are partitioned into equal shares of 8 objects each.

– continued on next page –

### Chapter 5 Division Concepts and Facts

PROGRESS IN MATHEMATICS, GRADE 3

**5-9**     **Function Machines**—pp. 178–179

**5-10**    **Problem Solving Strategy: Write a Number Sentence**—pp. 180–181

**5-11**    **Problem Solving Applications: Mixed Review**—pp. 182–183

COMMON CORE PROGRESS MATHEMATICS, GRADE 3

**Lesson 3**    **Problem Solving: Multiplication/Division and Equal Groups**—pp. 26–33

**Lesson 4**    **Problem Solving: Multiplication/Division and Arrays**—pp. 34–41

**Lesson 32**   **Problem Solving: Measurement**—pp. 288–295

**Lesson 3**    **Problem Solving: Multiplication/Division and Equal Groups**—pp. 26–33

**Lesson 4**    **Problem Solving: Multiplication/Division and Arrays**—pp. 34–41

**Lesson 32**   **Problem Solving: Measurement**—pp. 288–295

COMMON CORE STATE STANDARDS FOR MATHEMATICS, GRADE 3

– continued from previous page –

*For example, describe a context in which a number of shares or a number of groups can be expressed as  $56 \div 8$ .*

3.OA.3    Use multiplication and division within 100 to solve word problems in situations involving equal groups, arrays, and measurement quantities, e.g., by using drawings and equations with a symbol for the unknown number to represent the problem.

3.OA.3    Use multiplication and division within 100 to solve word problems in situations involving equal groups, arrays, and measurement quantities, e.g., by using drawings and equations with a symbol for the unknown number to represent the problem.

### Chapter 6 More Multiplication and Division Facts

PROGRESS IN MATHEMATICS, GRADE 3

**6-1**     **Factors and Products**—p. 190

COMMON CORE PROGRESS MATHEMATICS, GRADE 3

**Lesson 1**    **Interpret Products of Whole Numbers**—pp. 10–17

COMMON CORE STATE STANDARDS FOR MATHEMATICS, GRADE 3

3.OA.1    Interpret products of whole numbers, e.g., interpret  $5 \times 7$  as the total number of objects in 5 groups of 7 objects each.

*For example, describe a context in which a total number of objects can be expressed as  $5 \times 7$ .*

## Chapter 6 More Multiplication and Division Facts

PROGRESS IN MATHEMATICS, GRADE 3	COMMON CORE PROGRESS MATHEMATICS, GRADE 3	COMMON CORE STATE STANDARDS FOR MATHEMATICS, GRADE 3
<b>6-2</b> <b>Multiply Sixes</b> —p. 191	<b>Lesson 1</b> <b>Interpret Products of Whole Numbers</b> —pp. 10–17	3.OA.1    Interpret products of whole numbers, e.g., interpret $5 \times 7$ as the total number of objects in 5 groups of 7 objects each.
<b>6-3</b> <b>Multiply Sevens</b> —pp. 192–193		<i>For example, describe a context in which a total number of objects can be expressed as <math>5 \times 7</math>.</i>
	<b>Lesson 12</b> <b>Identify and Explain Arithmetic Patterns</b> —pp. 104–111	3.OA.9    Identify arithmetic patterns (including patterns in the addition table or multiplication table), and explain them using properties of operations.  <i>For example, observe that 4 times a number is always even, and explain why 4 times a number can be decomposed into two equal addends.</i>
<b>6-4</b> <b>Multiply Eights</b> —pp. 194–195	<b>Lesson 1</b> <b>Interpret Products of Whole Numbers</b> —pp. 10–17	3.OA.1    Interpret products of whole numbers, e.g., interpret $5 \times 7$ as the total number of objects in 5 groups of 7 objects each.
		<i>For example, describe a context in which a total number of objects can be expressed as <math>5 \times 7</math>.</i>
	<b>Lesson 3</b> <b>Problem Solving: Multiplication/Division and Equal Groups</b> —pp. 26–33	3.OA.3    Use multiplication and division within 100 to solve word problems in situations involving equal groups, arrays, and measurement quantities, e.g., by using drawings and equations with a symbol for the unknown number to represent the problem.
	<b>Lesson 4</b> <b>Problem Solving: Multiplication/Division and Arrays</b> —pp. 34–41	
	<b>Lesson 32</b> <b>Problem Solving: Measurement</b> —pp. 288–295	
	<b>Lesson 10</b> <b>Problem Solving: Two-Step Problems</b> —pp. 88–95	3.OA.8    Solve two-step word problems using the four operations. Represent these problems using equations with a letter standing for the unknown quantity. Assess the reasonableness of answers using mental computation and estimation strategies including rounding. <sup>3</sup>
		<sup>3</sup> This standard is limited to problems posed with whole numbers and having whole-number answers;
		– continued on next page –

## Chapter 6 More Multiplication and Division Facts

PROGRESS IN MATHEMATICS, GRADE 3	COMMON CORE PROGRESS MATHEMATICS, GRADE 3	COMMON CORE STATE STANDARDS FOR MATHEMATICS, GRADE 3
		– continued from previous page –
		students should know how to perform operations in the conventional order when there are no parentheses to specify a particular order (Order of Operations).
	<b>Lesson 12 Identify and Explain Arithmetic Patterns</b> —pp. 104–111	3.OA.9 Identify arithmetic patterns (including patterns in the addition table or multiplication table), and explain them using properties of operations.  <i>For example, observe that 4 times a number is always even, and explain why 4 times a number can be decomposed into two equal addends.</i>
<b>6-5 Multiply Nines</b> —pp. 196–197	<b>Lesson 1 Interpret Products of Whole Numbers</b> —pp. 10–17	3.OA.1 Interpret products of whole numbers, e.g., interpret $5 \times 7$ as the total number of objects in 5 groups of 7 objects each.  <i>For example, describe a context in which a total number of objects can be expressed as <math>5 \times 7</math>.</i>
	<b>Lesson 12 Identify and Explain Arithmetic Patterns</b> —pp. 104–111	3.OA.9 Identify arithmetic patterns (including patterns in the addition table or multiplication table), and explain them using properties of operations.  <i>For example, observe that 4 times a number is always even, and explain why 4 times a number can be decomposed into two equal addends.</i>
<b>*6-5A Break Apart Numbers to Multiply</b> —Online	<b>Lesson 3 Problem Solving: Multiplication/Division and Equal Groups</b> —pp. 26–33	3.OA.3 Use multiplication and division within 100 to solve word problems in situations involving equal groups, arrays, and measurement quantities, e.g., by using drawings and equations with a symbol for the unknown number to represent the problem.
	<b>Lesson 4 Problem Solving: Multiplication/Division and Arrays</b> —pp. 34–41	
	<b>Lesson 32 Problem Solving: Measurement</b> —pp. 288–295	

**Chapter 6 More Multiplication and Division Facts**

PROGRESS IN MATHEMATICS, GRADE 3

**\*6-5B Multiplication Tables**—Online

**6-6 Multiply Three Numbers**—pp. 198–199

COMMON CORE PROGRESS MATHEMATICS, GRADE 3

**Lesson 6 Apply Commutative and Associative Properties to Multiply**—pp. 50–57

**Lesson 7 Apply the Distributive Property to Multiply**—pp. 58–65

**Lesson 9 Multiply and Divide Fluently within 100**—pp. 80–87

**Lesson 12 Identify and Explain Arithmetic Patterns**—pp. 104–111

**Lesson 6 Apply Commutative and Associative Properties to Multiply**—pp. 50–57

**Lesson 7 Apply the Distributive Property to Multiply**—pp. 58–65

COMMON CORE STATE STANDARDS FOR MATHEMATICS, GRADE 3

3.OA.5 Apply properties of operations as strategies to multiply and divide.<sup>2</sup>

*Examples: If  $6 \times 4 = 24$  is known, then  $4 \times 6 = 24$  is also known. (Commutative property of multiplication.)  $3 \times 5 \times 2$  can be found by  $3 \times 5 = 15$ , then  $15 \times 2 = 30$ , or by  $5 \times 2 = 10$ , then  $3 \times 10 = 30$ . (Associative property of multiplication.) Knowing that  $8 \times 5 = 40$  and  $8 \times 2 = 16$ , one can find  $8 \times 7$  as  $8 \times (5 + 2) = (8 \times 5) + (8 \times 2) = 40 + 16 = 56$ . (Distributive property.)*

<sup>2</sup>Students need not use formal terms for these properties.

3.OA.7 Fluently multiply and divide within 100, using strategies such as the relationship between multiplication and division (e.g., knowing that  $8 \times 5 = 40$ , one knows  $40 \div 5 = 8$ ) or properties of operations. By the end of Grade 3, know from memory all products of two one-digit numbers. Solve problems involving the four operations, and identify and explain patterns in arithmetic.

3.OA.9 Identify arithmetic patterns (including patterns in the addition table or multiplication table), and explain them using properties of operations.

*For example, observe that 4 times a number is always even, and explain why 4 times a number can be decomposed into two equal addends.*

3.OA.5 Apply properties of operations as strategies to multiply and divide.<sup>2</sup>

*Examples: If  $6 \times 4 = 24$  is known, then  $4 \times 6 = 24$  is also known. (Commutative property of multiplication.)  $3 \times 5 \times 2$  can be found by  $3 \times 5 =$*

– continued on next page –

## Chapter 6 More Multiplication and Division Facts

PROGRESS IN MATHEMATICS, GRADE 3

COMMON CORE PROGRESS MATHEMATICS, GRADE 3

COMMON CORE STATE STANDARDS FOR MATHEMATICS, GRADE 3

– continued from previous page –

15, then  $15 \times 2 = 30$ , or by  $5 \times 2 = 10$ , then  $3 \times 10 = 30$ . (Associative property of multiplication.)  
Knowing that  $8 \times 5 = 40$  and  $8 \times 2 = 16$ , one can find  $8 \times 7$  as  $8 \times (5 + 2) = (8 \times 5) + (8 \times 2) = 40 + 16 = 56$ . (Distributive property.)

<sup>2</sup>Students need not use formal terms for these properties.

**6-7** **Division Review**—pp. 200–201

**Lesson 2** **Interpret Quotients of Whole Numbers**—pp. 18–26

3.OA.2 Interpret whole-number quotients of whole numbers, e.g., interpret  $56 \div 8$  as the number of objects in each share when 56 objects are partitioned equally into 8 shares, or as a number of shares when 56 objects are partitioned into equal shares of 8 objects each.

For example, describe a context in which a number of shares or a number of groups can be expressed as  $56 \div 8$ .

**Lesson 6** **Apply Commutative and Associative Properties to Multiply**—pp. 50–57

3.OA.5 Apply properties of operations as strategies to multiply and divide.<sup>2</sup>

**Lesson 7** **Apply the Distributive Property to Multiply**—pp. 58–65

Examples: If  $6 \times 4 = 24$  is known, then  $4 \times 6 = 24$  is also known. (Commutative property of multiplication.)  $3 \times 5 \times 2$  can be found by  $3 \times 5 = 15$ , then  $15 \times 2 = 30$ , or by  $5 \times 2 = 10$ , then  $3 \times 10 = 30$ . (Associative property of multiplication.)  
Knowing that  $8 \times 5 = 40$  and  $8 \times 2 = 16$ , one can find  $8 \times 7$  as  $8 \times (5 + 2) = (8 \times 5) + (8 \times 2) = 40 + 16 = 56$ . (Distributive property.)

<sup>2</sup>Students need not use formal terms for these properties.

**Lesson 9** **Multiply and Divide Fluently within 100**—pp. 80–87

3.OA.7 Fluently multiply and divide within 100, using strategies such as the relationship between multiplication and division (e.g., knowing that

– continued on next page –

**Chapter 6 More Multiplication and Division Facts**

PROGRESS IN MATHEMATICS, GRADE 3

<b>6-8</b>	<b>Divide by 6</b> —pp. 202–203
<b>6-9</b>	<b>Divide by 7</b> —pp. 204–205
<b>6-10</b>	<b>Divide by 8</b> —pp. 206–207
<b>6-11</b>	<b>Divide by 9</b> —pp. 208–209

<b>6-12</b>	<b>Operation Patterns</b> —pp. 210–211
-------------	--

COMMON CORE PROGRESS MATHEMATICS, GRADE 3

<b>Lesson 2</b>	<b>Interpret Quotients of Whole Numbers</b> —pp. 18–26
-----------------	--

<b>Lesson 12</b>	<b>Identify and Explain Arithmetic Patterns</b> —pp. 104–111
------------------	--

<b>Lesson 12</b>	<b>Identify and Explain Arithmetic Patterns</b> —pp. 104–111
------------------	--

COMMON CORE STATE STANDARDS FOR MATHEMATICS, GRADE 3

– continued from previous page –

$8 \times 5 = 40$ , one knows  $40 \div 5 = 8$ ) or properties of operations. By the end of Grade 3, know from memory all products of two one-digit numbers. Solve problems involving the four operations, and identify and explain patterns in arithmetic.

3.OA.2	Interpret whole-number quotients of whole numbers, e.g., interpret $56 \div 8$ as the number of objects in each share when 56 objects are partitioned equally into 8 shares, or as a number of shares when 56 objects are partitioned into equal shares of 8 objects each.
--------	--

*For example, describe a context in which a number of shares or a number of groups can be expressed as  $56 \div 8$ .*

3.OA.9	Identify arithmetic patterns (including patterns in the addition table or multiplication table), and explain them using properties of operations.
--------	---

*For example, observe that 4 times a number is always even, and explain why 4 times a number can be decomposed into two equal addends.*

3.OA.9	Identify arithmetic patterns (including patterns in the addition table or multiplication table), and explain them using properties of operations.
--------	---

*For example, observe that 4 times a number is always even, and explain why 4 times a number can be decomposed into two equal addends.*

**Chapter 6 More Multiplication and Division Facts**

PROGRESS IN MATHEMATICS, GRADE 3

**\*6-12A Missing Operands: Multiplication & Division—**  
Online

**6-13 Fact Families—**pp. 212–213

COMMON CORE PROGRESS MATHEMATICS, GRADE 3

**Lesson 3 Problem Solving: Multiplication/Division and Equal Groups—**pp. 26–33

**Lesson 4 Problem Solving: Multiplication/Division and Arrays—**pp. 34–41

**Lesson 32 Problem Solving: Measurement—**pp. 288–295

**Lesson 5 Find Unknown Numbers in Multiplication and Division Equations—**pp. 42–49

**Lesson 5 Find Unknown Numbers in Multiplication and Division Equations—**pp. 42–49

**Lesson 6 Apply Commutative and Associative Properties to Multiply—**pp. 50–57

**Lesson 7 Apply the Distributive Property to Multiply—**pp. 58–65

COMMON CORE STATE STANDARDS FOR MATHEMATICS, GRADE 3

3.OA.3 Use multiplication and division within 100 to solve word problems in situations involving equal groups, arrays, and measurement quantities, e.g., by using drawings and equations with a symbol for the unknown number to represent the problem.

3.OA.4 Determine the unknown whole number in a multiplication or division equation relating three whole numbers.

*For example, determine the unknown number that makes the equation true in each of the equations  $8 \times ? = 48$ ,  $5 = \square \div 3$ ,  $6 \times 6 = ?$ .*

3.OA.4 Determine the unknown whole number in a multiplication or division equation relating three whole numbers.

*For example, determine the unknown number that makes the equation true in each of the equations  $8 \times ? = 48$ ,  $5 = \square \div 3$ ,  $6 \times 6 = ?$ .*

3.OA.5 Apply properties of operations as strategies to multiply and divide.<sup>2</sup>

*Examples: If  $6 \times 4 = 24$  is known, then  $4 \times 6 = 24$  is also known. (Commutative property of multiplication.)  $3 \times 5 \times 2$  can be found by  $3 \times 5 = 15$ , then  $15 \times 2 = 30$ , or by  $5 \times 2 = 10$ , then  $3 \times 10 = 30$ . (Associative property of multiplication.) Knowing that  $8 \times 5 = 40$  and  $8 \times 2 = 16$ , one can find  $8 \times 7$  as  $8 \times (5 + 2) = (8 \times 5) + (8 \times 2) = 40 + 16 = 56$ . (Distributive property.)*

<sup>2</sup>Students need not use formal terms for these properties.

## Chapter 6 More Multiplication and Division Facts

PROGRESS IN MATHEMATICS, GRADE 3	COMMON CORE PROGRESS MATHEMATICS, GRADE 3	COMMON CORE STATE STANDARDS FOR MATHEMATICS, GRADE 3
	<p><b>Lesson 8 Divide by Finding an Unknown Factor</b>—pp. 66–73</p>	<p>3.OA.6 Understand division as an unknown-factor problem.</p> <p><i>For example, find <math>32 \div 8</math> by finding the number that makes 32 when multiplied by 8. Multiply and divide within 100.</i></p>
	<p><b>Lesson 9 Multiply and Divide Fluently within 100</b>—pp. 80–87</p>	<p>3.OA.7 Fluently multiply and divide within 100, using strategies such as the relationship between multiplication and division (e.g., knowing that <math>8 \times 5 = 40</math>, one knows <math>40 \div 5 = 8</math>) or properties of operations. By the end of Grade 3, know from memory all products of two one-digit numbers. Solve problems involving the four operations, and identify and explain patterns in arithmetic.</p>
<p><b>6-14 Apply Facts</b>—pp. 214–215</p>	<p><b>Lesson 3 Problem Solving: Multiplication/Division and Equal Groups</b>—pp. 26–33</p>	<p>3.OA.3 Use multiplication and division within 100 to solve word problems in situations involving equal groups, arrays, and measurement quantities, e.g., by using drawings and equations with a symbol for the unknown number to represent the problem.</p>
	<p><b>Lesson 4 Problem Solving: Multiplication/Division and Arrays</b>—pp. 34–41</p>	<p>3.OA.8 Solve two-step word problems using the four operations. Represent these problems using equations with a letter standing for the unknown quantity. Assess the reasonableness of answers using mental computation and estimation strategies including rounding.<sup>3</sup></p> <p><sup>3</sup>This standard is limited to problems posed with whole numbers and having whole-number answers; students should know how to perform operations in the conventional order when there are no parentheses to specify a particular order (Order of Operations).</p>
<p><b>*6-14A Checking Reasonableness of Answers</b>—Online</p>	<p><b>Lesson 32 Problem Solving: Measurement</b>—pp. 288–295</p>	
<p><b>*6-14B Writing Variable Expressions</b>—Online</p>	<p><b>Lesson 10 Problem Solving: Two-Step Problems</b>—pp. 88–95</p>	

## Chapter 6 More Multiplication and Division Facts

PROGRESS IN MATHEMATICS, GRADE 3		COMMON CORE PROGRESS MATHEMATICS, GRADE 3		COMMON CORE STATE STANDARDS FOR MATHEMATICS, GRADE 3	
<b>6-15</b>	<b>Problem Solving Strategy: Guess and Test</b> —pp. 216–217	<b>Lesson 3</b>	<b>Problem Solving: Multiplication/Division and Equal Groups</b> —pp. 26–33	3.OA.3	Use multiplication and division within 100 to solve word problems in situations involving equal groups, arrays, and measurement quantities, e.g., by using drawings and equations with a symbol for the unknown number to represent the problem.
<b>6-16</b>	<b>Problem Solving Applications: Mixed Review</b> —pp. 218–219	<b>Lesson 4</b>	<b>Problem Solving: Multiplication/Division and Arrays</b> —pp. 34–41		
		<b>Lesson 32</b>	<b>Problem Solving: Measurement</b> —pp. 288–295		
		<b>Lesson 10</b>	<b>Problem Solving: Two-Step Problems</b> —pp. 88–95	3.OA.8	Solve two-step word problems using the four operations. Represent these problems using equations with a letter standing for the unknown quantity. Assess the reasonableness of answers using mental computation and estimation strategies including rounding. <sup>3</sup>  <sup>3</sup> This standard is limited to problems posed with whole numbers and having whole-number answers; students should know how to perform operations in the conventional order when there are no parentheses to specify a particular order (Order of Operations).

## Chapter 7 Statistics and Probability

PROGRESS IN MATHEMATICS, GRADE 3		COMMON CORE PROGRESS MATHEMATICS, GRADE 3		COMMON CORE STATE STANDARDS FOR MATHEMATICS, GRADE 3	
<b>7-1</b>	<b>Pictographs</b> —pp. 226–227	<b>Lesson 26</b>	<b>Draw Graphs to Represent Categorical Data</b> —pp. 234–241	3.MD.3	Draw a scaled picture graph and a scaled bar graph to represent a data set with several categories. Solve one- and two-step “how many more” and “how many less” problems using information presented in scaled bar graphs.  <i>For example, draw a bar graph in which each square in the bar graph might represent 5 pets.</i>
<b>7-2</b>	<b>Bar Graphs</b> —pp. 228–229				
<b>*7-2A</b>	<b>Data and Two-Step Problems</b> —Online				
<b>7-3</b>	<b>Surveys</b> —pp. 230–231				
<b>7-4</b>	<b>Circle Graphs</b> —pp. 232–233				
<b>7-5</b>	<b>Line Plots</b> —pp. 234–235				

## Chapter 7 Statistics and Probability

PROGRESS IN MATHEMATICS, GRADE 3	COMMON CORE PROGRESS MATHEMATICS, GRADE 3	COMMON CORE STATE STANDARDS FOR MATHEMATICS, GRADE 3
<b>7-6</b> <b>Line Graphs</b> —pp. 236–237	<b>Lesson 26</b> <b>Draw Graphs to Represent Categorical Data</b> —pp. 234–241	3.MD.3    Draw a scaled picture graph and a scaled bar graph to represent a data set with several categories. Solve one- and two-step “how many more” and “how many less” problems using information presented in scaled bar graphs.  <i>For example, draw a bar graph in which each square in the bar graph might represent 5 pets.</i>
<b>7-7</b> <b>Median and Mean</b> —pp. 238–239		
<b>7-8</b> <b>Compare Data</b> —pp. 240–241	<b>Lesson 26</b> <b>Draw Graphs to Represent Categorical Data</b> —pp. 234–241	3.MD.3    Draw a scaled picture graph and a scaled bar graph to represent a data set with several categories. Solve one- and two-step “how many more” and “how many less” problems using information presented in scaled bar graphs.  <i>For example, draw a bar graph in which each square in the bar graph might represent 5 pets.</i>
<b>7-9</b> <b>Arrangements and Combinations</b> —pp. 242–243		
<b>7-10</b> <b>Probability Experiments Events and Outcomes</b> —pp. 244–245		
<b>7-11</b> <b>Graph Results of Probability Experiments</b> —pp. 246–247		
<b>7-12</b> <b>Make Predictions</b> —pp. 248–249		
<b>7-13</b> <b>Problem Solving Strategy: Use a Graph</b> —pp. 250–251	<b>Lesson 26</b> <b>Draw Graphs to Represent Categorical Data</b> —pp. 234–241	3.MD.3    Draw a scaled picture graph and a scaled bar graph to represent a data set with several categories. Solve one- and two-step “how many more” and “how many less” problems using information presented in scaled bar graphs.
<b>7-14</b> <b>Problem Solving Applications: Mixed Review</b> —pp. 252–253		<i>For example, draw a bar graph in which each square in the bar graph might represent 5 pets.</i>

## Chapter 8 Measurement and Time

PROGRESS IN MATHEMATICS, GRADE 3	COMMON CORE PROGRESS MATHEMATICS, GRADE 3	COMMON CORE STATE STANDARDS FOR MATHEMATICS, GRADE 3
<p><b>8-1 Quarter Inch, Half Inch, Inch</b>—pp. 260–261</p>	<p><b>Lesson 27 Generate and Graph Measurement Data</b>—pp. 242–249</p>	<p>3.MD.4 Generate measurement data by measuring lengths using rulers marked with halves and fourths of an inch. Show the data by making a line plot, where the horizontal scale is marked off in appropriate units—whole numbers, halves, or quarters.</p>
<p><b>8-2 Foot, Yard</b>—pp. 262–263</p>		
<p><b>8-3 Mile</b>—pp. 264–265</p>		
<p><b>8-4 Customary Units of Capacity</b>—pp. 266–267</p>		
<p><b>8-5 Ounce, Pound</b>—pp. 268–269</p>		
<p><b>8-6 Metric Units of Length</b>—pp. 270–271</p>		
<p><b>8-7 Meter</b>—pp. 272–273</p>		
<p><b>8-8 Kilometer</b>—pp. 274–275</p>		
<p><b>8-9 Milliliter, Liter</b>—pp. 276–277</p>	<p><b>Lesson 25 Problem Solving: Volumes and Masses</b>—pp. 226–233</p>	
<p><b>8-10 Gram, Kilogram</b>—pp. 278–279</p>	<p><b>Lesson 32 Problem Solving: Measurement</b>—pp. 288–295</p>	<p>3.MD.2 Measure and estimate liquid volumes and masses of objects using standard units of grams (g), kilograms (kg), and liters (l).<sup>6</sup> Add, subtract, multiply, or divide to solve one-step word problems involving masses or volumes that are such as a beaker with a measurement scale) to represent the problem.<sup>7</sup></p>
<p><b>*8-10A Estimate and Measure Masses</b>—Online</p>		<p><sup>6</sup>Excludes compound units such as <math>\text{cm}^3</math> and finding the geometric volume of a container.</p>
		<p><sup>7</sup>Excludes multiplicative comparison problems (problems involving notions of “times as much.”)</p>
	<p><b>Lesson 3 Problem Solving: Multiplication/Division and Equal Groups</b>—pp. 26–33</p>	
	<p><b>Lesson 4 Problem Solving: Multiplication/Division and Arrays</b>—pp. 34–41</p>	<p>3.OA.3 Use multiplication and division within 100 to solve word problems in situations involving equal groups, arrays, and measurement quantities, e.g., by using drawings and equations with a symbol for the unknown number to represent the problem.</p>
	<p><b>Lesson 32 Problem Solving: Measurement</b>—pp. 288–295</p>	
<p><b>8-11 Rename Units of Measure</b>—pp. 280–281</p>		

### Chapter 8 Measurement and Time

PROGRESS IN MATHEMATICS, GRADE 3

**8-12 Choose the Measuring Tool**—pp. 282–283

**\*8-12A Collect and Represent Data**—Online

**8-13 Temperature**—pp. 284–285

**8-14 Quarter Hour**—pp. 286–287

COMMON CORE PROGRESS MATHEMATICS, GRADE 3

**Lesson 10 Problem Solving: Two-Step Problems**—pp. 88–95

**Lesson 25 Problem Solving: Volumes and Masses**—pp. 226–233

**Lesson 32 Problem Solving: Measurement**—pp. 288–295

**Lesson 27 Generate and Graph Measurement Data**—pp. 242–249

COMMON CORE STATE STANDARDS FOR MATHEMATICS, GRADE 3

**3.OA.8** Solve two-step word problems using the four operations. Represent these problems using equations with a letter standing for the unknown quantity. Assess the reasonableness of answers using mental computation and estimation strategies including rounding.<sup>3</sup>

<sup>3</sup>This standard is limited to problems posed with whole numbers and having whole-number answers; students should know how to perform operations in the conventional order when there are no parentheses to specify a particular order (Order of Operations).

**3.MD.2** Measure and estimate liquid volumes and masses of objects using standard units of grams (g), kilograms (kg), and liters (l).<sup>6</sup> Add, subtract, multiply, or divide to solve one-step word problems involving masses or volumes that are such as a beaker with a measurement scale) to represent the problem.<sup>7</sup>

<sup>6</sup>Excludes compound units such as cm<sup>3</sup> and finding the geometric volume of a container.

<sup>7</sup>Excludes multiplicative comparison problems (problems involving notions of “times as much.”)

**3.MD.4** Generate measurement data by measuring lengths using rulers marked with halves and fourths of an inch. Show the data by making a line plot, where the horizontal scale is marked off in appropriate units—whole numbers, halves, or quarters.

## Chapter 8 Measurement and Time

PROGRESS IN MATHEMATICS, GRADE 3	
<b>8-15</b>	<b>Minutes</b> —pp. 288–289
<b>8-16</b>	<b>Elapsed Time</b> —pp. 290–291
<b>*8-16A</b>	<b>Time on a Number Line</b> —Online
<b>8-17</b>	<b>Calendar</b> —pp. 292–293
<b>8-18</b>	<b>Problem Solving Strategy: Make a Table</b> —pp. 294–295
<b>8-19</b>	<b>Problem Solving Applications: Mixed Review</b> —pp. 296–297

## Chapter 9 Geometry

PROGRESS IN MATHEMATICS, GRADE 3	
<b>9-1</b>	<b>Lines</b> —pp. 304–305
<b>9-2</b>	<b>Angles</b> —pp. 306–307
<b>9-3</b>	<b>Polygons and Circles</b> —pp. 308–309
<b>9-4</b>	<b>Triangles</b> —pp. 310–311
<b>*9-4A</b>	<b>Quadrilaterals</b> —Online

COMMON CORE PROGRESS MATHEMATICS, GRADE 3	
<b>Lesson 24</b>	<b>Problem Solving: Time</b> —pp. 218–225
<b>Lesson 25</b>	<b>Problem Solving: Volumes and Masses</b> —pp. 226–233
<b>Lesson 32</b>	<b>Problem Solving: Measurement</b> —pp. 288–295
<b>Lesson 35</b>	<b>Understand Shapes and Attributes</b> —pp. 312–319

COMMON CORE STATE STANDARDS FOR MATHEMATICS, GRADE 3	
3.MD.1	Tell and write time to the nearest minute and measure time intervals in minutes. Solve word problems involving addition and subtraction of time intervals in minutes, e.g., by representing the problem on a number line diagram.
3.MD.2	Measure and estimate liquid volumes and masses of objects using standard units of grams (g), kilograms (kg), and liters (l). <sup>6</sup> Add, subtract, multiply, or divide to solve one-step word problems involving masses or volumes that are such as a beaker with a measurement scale) to represent the problem. <sup>7</sup>  <sup>6</sup> Excludes compound units such as $\text{cm}^3$ and finding the geometric volume of a container.  <sup>7</sup> Excludes multiplicative comparison problems (problems involving notions of “times as much.”)
3.G.1	Understand that shapes in different categories (e.g., rhombuses, rectangles, and others) may share attributes (e.g., having four sides), and that the shared attributes can define a larger category (e.g., quadrilaterals). Recognize rhombuses, rectangles, and squares as examples of quadrilaterals, and draw examples of quadrilaterals that do not belong to any of these subcategories.

## Chapter 9 Geometry

PROGRESS IN MATHEMATICS, GRADE 3	COMMON CORE PROGRESS MATHEMATICS, GRADE 3	COMMON CORE STATE STANDARDS FOR MATHEMATICS, GRADE 3
<b>9-5</b> <b>Congruent and Similar Figures</b> —pp. 312–313		
<b>9-6</b> <b>Ordered Pairs</b> —pp. 314–315		
<b>9-7</b> <b>Symmetry</b> —p. 316	<b>Lesson 36</b> <b>Partition Shapes to Make Equal Areas</b> — pp. 320–327	3.G.2    Partition shapes into parts with equal areas. Express the area of each part as a unit fraction of the whole.  <i>For example, partition a shape into 4 parts with equal area, and describe the area of each part as 1/4 of the area of the shape.</i>
<b>9-8</b> <b>Transformations</b> —p. 317		
<b>9-9</b> <b>Solid Figures</b> —pp. 318–319		
<b>9-10</b> <b>Perimeter</b> —pp. 320–321	<b>Lesson 33</b> <b>Problem Solving: Perimeter</b> —pp. 296–303  <b>Lesson 34</b> <b>Problem Solving: Compare Perimeter and Area</b> —pp. 304–311	3.MD.8    Solve real world and mathematical problems involving perimeters of polygons, including finding the perimeter given the side lengths, finding an unknown side length, and exhibiting rectangles with the same perimeter and different areas or with the same area and different perimeters.
<b>9-11</b> <b>Area</b> —pp. 322–323	<b>Lesson 28</b> <b>Understand Concepts of Area Measurement</b> —pp. 256–263	3.MD.5a    A square with side length 1 unit, called “a unit square,” is said to have “one square unit” of area, and can be used to measure area.
<b>*9-11A</b> <b>Area of a Rectangle</b> —Online		3.MD.5b    A plane figure which can be covered without gaps or overlaps by $n$ unit squares is said to have an area of $n$ square units.  3.MD.6    Measure areas by counting unit squares (square cm, square m, square in, square ft, and improvised units).

## Chapter 9 Geometry

## PROGRESS IN MATHEMATICS, GRADE 3

## COMMON CORE PROGRESS MATHEMATICS, GRADE 3

**Lesson 29 Find Areas of Rectangles: Tile and Multiply**—pp. 264–271

**Lesson 33 Problem Solving: Perimeter**—pp. 296–303

**Lesson 34 Problem Solving: Compare Perimeter and Area**—pp. 304–311

**\*9-11B Area of Composite Shapes**—Online

**Lesson 29 Find Areas of Rectangles: Tile and Multiply**—pp. 264–271

**Lesson 30 Find Areas of Rectangles: Use the Distributive Property**—pp. 272–279

**Lesson 32 Problem Solving: Measurement**—pp. 288–295

**Lesson 31 Find Areas: Decompose Figures into Rectangles**—pp. 280–287

**Lesson 32 Problem Solving: Measurement**—pp. 288–295

## COMMON CORE STATE STANDARDS FOR MATHEMATICS, GRADE 3

3.MD.7a Find the area of a rectangle with whole-number side lengths by tiling it, and show that the area is the same as would be found by multiplying the side lengths.

3.MD.7b Multiply side lengths to find areas of rectangles with whole-number side lengths in the context of solving real world and mathematical problems, and represent whole-number products as rectangular areas in mathematical reasoning.

3.MD.8 Solve real world and mathematical problems involving perimeters of polygons, including finding the perimeter given the side lengths, finding an unknown side length, and exhibiting rectangles with the same perimeter and different areas or with the same area and different perimeters.

3.MD.7b Multiply side lengths to find areas of rectangles with whole-number side lengths in the context of solving real world and mathematical problems, and represent whole-number products as rectangular areas in mathematical reasoning.

3.MD.7c Use tiling to show in a concrete case that the area of a rectangle with whole-number side lengths  $a$  and  $b + c$  is the sum of  $a \times b$  and  $a \times c$ . Use area models to represent the distributive property in mathematical reasoning.

3.MD.7d Recognize area as additive. Find areas of rectilinear figures by decomposing them into non-overlapping rectangles and adding the areas of the non-overlapping parts, applying this technique to solve real world problems.

### Chapter 9 Geometry

PROGRESS IN MATHEMATICS, GRADE 3

\*9-11C Perimeter and Area—Online

\*9-11D Missing Dimensions—Online

9-12 Volume—pp. 324–325

\*9-12A Estimate and Measure Volume—Online

\*9-12B Measurement Problems—Online

COMMON CORE PROGRESS MATHEMATICS, GRADE 3

**Lesson 33 Problem Solving: Perimeter**—pp. 296–303

**Lesson 34 Problem Solving: Compare Perimeter and Area**—pp. 304–311

**Lesson 33 Problem Solving: Perimeter**—pp. 296–303

**Lesson 34 Problem Solving: Compare Perimeter and Area**—pp. 304–311

**Lesson 25 Problem Solving: Volumes and Masses**—pp. 226–233

**Lesson 32 Problem Solving: Measurement**—pp. 288–295

**Lesson 3 Problem Solving: Multiplication/Division and Equal Groups**—pp. 26–33

**Lesson 4 Problem Solving: Multiplication/Division and Arrays**—pp. 34–41

**Lesson 32 Problem Solving: Measurement**—pp. 288–295

COMMON CORE STATE STANDARDS FOR MATHEMATICS, GRADE 3

3.MD.8 Solve real world and mathematical problems involving perimeters of polygons, including finding the perimeter given the side lengths, finding an unknown side length, and exhibiting rectangles with the same perimeter and different areas or with the same area and different perimeters.

3.MD.8 Solve real world and mathematical problems involving perimeters of polygons, including finding the perimeter given the side lengths, finding an unknown side length, and exhibiting rectangles with the same perimeter and different areas or with the same area and different perimeters.

3.MD.2 Measure and estimate liquid volumes and masses of objects using standard units of grams (g), kilograms (kg), and liters (l).<sup>6</sup> Add, subtract, multiply, or divide to solve one-step word problems involving masses or volumes that are such as a beaker with a measurement scale) to represent the problem.<sup>7</sup>

<sup>6</sup>Excludes compound units such as cm<sup>3</sup> and finding the geometric volume of a container.

<sup>7</sup>Excludes multiplicative comparison problems (problems involving notions of “times as much.”)

3.OA.3 Use multiplication and division within 100 to solve word problems in situations involving equal groups, arrays, and measurement quantities, e.g., by using drawings and equations with a symbol for the unknown number to represent the problem.

## Chapter 9 Geometry

PROGRESS IN MATHEMATICS, GRADE 3	COMMON CORE PROGRESS MATHEMATICS, GRADE 3	COMMON CORE STATE STANDARDS FOR MATHEMATICS, GRADE 3
	<p><b>Lesson 25 Problem Solving: Volumes and Masses</b>—pp. 226–233</p>	<p>3.MD.2 Measure and estimate liquid volumes and masses of objects using standard units of grams (g), kilograms (kg), and liters (l).<sup>6</sup> Add, subtract, multiply, or divide to solve one-step word problems involving masses or volumes that are such as a beaker with a measurement scale) to represent the problem.<sup>7</sup></p> <p><sup>6</sup>Excludes compound units such as <math>\text{cm}^3</math> and finding the geometric volume of a container.</p> <p><sup>7</sup>Excludes multiplicative comparison problems (problems involving notions of “times as much.”)</p>
<p><b>9-13 Problem Solving Strategy: Solve a Simpler Problem</b>—pp. 326–327</p>	<p><b>Lesson 31 Find Areas: Decompose Figures into Rectangles</b>—pp. 280–287</p>	<p>3.MD.7d Recognize area as additive. Find areas of rectilinear figures by decomposing them into non-overlapping rectangles and adding the areas of the non-overlapping parts, applying this technique to solve real world problems.</p>
<p><b>9-14 Problem Solving Applications: Mixed Review</b>—pp. 328–329</p>	<p><b>Lesson 32 Problem Solving: Measurement</b>—pp. 288–295</p> <p><b>Lesson 35 Understand Shapes and Attributes</b>—pp. 312–319</p>	<p>3.G.1 Understand that shapes in different categories (e.g., rhombuses, rectangles, and others) may share attributes (e.g., having four sides), and that the shared attributes can define a larger category (e.g., quadrilaterals). Recognize rhombuses, rectangles, and squares as examples of quadrilaterals, and draw examples of quadrilaterals that do not belong to any of these subcategories.</p>

## Chapter 10 Multiply by One Digit

PROGRESS IN MATHEMATICS, GRADE 3	COMMON CORE PROGRESS MATHEMATICS, GRADE 3	COMMON CORE STATE STANDARDS FOR MATHEMATICS, GRADE 3
<p><b>10-1 Multiplication Patterns</b>—pp. 336–337</p>	<p><b>Lesson 12 Identify and Explain Arithmetic Patterns</b>—pp. 104–111</p>	<p>3.OA.9 Identify arithmetic patterns (including patterns in the addition table or multiplication table), and explain them using properties of operations.</p> <p><i>For example, observe that 4 times a number is always even, and explain why 4 times a number can be decomposed into two equal addends.</i></p>
<p><b>*10-1A Multiply with Multiples</b>—Online</p>		

### Chapter 10 Multiply by One Digit

PROGRESS IN MATHEMATICS, GRADE 3	COMMON CORE PROGRESS MATHEMATICS, GRADE 3	COMMON CORE STATE STANDARDS FOR MATHEMATICS, GRADE 3
<p><b>10-2 Estimate Products</b>—pp. 338–339</p>	<p><b>Lesson 15 Multiply One-Digit Whole Numbers by Multiples of 10</b>—pp. 128–135</p>	<p>3.NBT.3 Multiply one-digit whole numbers by multiples of 10 in the range 10–90 (e.g., <math>9 \times 80</math>, <math>5 \times 60</math>) using strategies based on place value and properties of operations.</p>
<p><b>10-3 Multiply Two Digits</b>—pp. 340–341</p>	<p><b>Lesson 13 Round Whole Numbers to the Nearest 10 or 100</b>—pp. 112–119</p>	<p>3.NBT.1 Use place value understanding to round whole numbers to the nearest 10 or 100.</p>
<p><b>10-4 Multiply with Models</b>—pp. 342–343</p>	<p><b>Lesson 15 Multiply One-Digit Whole Numbers by Multiples of 10</b>—pp. 128–135</p>	<p>3.NBT.3 Multiply one-digit whole numbers by multiples of 10 in the range 10–90 (e.g., <math>9 \times 80</math>, <math>5 \times 60</math>) using strategies based on place value and properties of operations.</p>
<p><b>10-5 Multiply with Regrouping</b>—pp. 344–345</p>	<p><b>Lesson 5 Find Unknown Numbers in Multiplication and Division Equations</b>—pp. 42–49</p>	<p>3.OA.4 Determine the unknown whole number in a multiplication or division equation relating three whole numbers.</p> <p><i>For example, determine the unknown number that makes the equation true in each of the equations <math>8 \times ? = 48</math>, <math>5 = \square \div 3</math>, <math>6 \times 6 = ?</math>.</i></p>
<p><b>10-6 More Multiplying with Regrouping</b>—pp. 346–347</p>		
<p><b>10-7 Multiply Three Digits</b>—pp. 348–349</p>		
<p><b>10-8 Regroup in Multiplication</b>—pp. 350–351</p>		
<p><b>10-9 Regroup Twice in Multiplication</b>—pp. 352–353</p>		
<p><b>10-10 Problem Solving Strategy: Work Backward</b>—pp. 354–355</p>		
<p><b>10-11 Problem Solving Applications: Mixed Review</b>—pp. 356–357</p>		

### Chapter 11 Divide by One Digit

PROGRESS IN MATHEMATICS, GRADE 3	
11-1	<b>Division Sense</b> —pp. 364–365
11-2	<b>Division with Remainders</b> —pp. 366–367
11-3	<b>One-Digit Quotients</b> —pp. 368–369
11-4	<b>Two-Digit Quotients</b> —pp. 370–371
11-5	<b>Quotients with Remainders</b> —pp. 372–373
11-6	<b>Estimate Quotients</b> —pp. 374–375
11-7	<b>Problem Solving Strategy: Interpret the Remainder</b> —pp. 376–377
11-8	<b>Problem Solving Applications: Mixed Review</b> —pp. 378–379

COMMON CORE PROGRESS MATHEMATICS, GRADE 3	

COMMON CORE STATE STANDARDS FOR MATHEMATICS, GRADE 3	

### Chapter 12 Fractions

PROGRESS IN MATHEMATICS, GRADE 3	
12-1	<b>Fractions</b> —pp. 386–387

COMMON CORE PROGRESS MATHEMATICS, GRADE 3	
<b>Lesson 16</b>	<b>Understand Unit Fractions as Quantities</b> —pp. 142–149
<b>Lesson 17</b>	<b>Understand Fractions as Quantities</b> —pp. 150–157
<b>Lesson 36</b>	<b>Partition Shapes to Make Equal Areas</b> —pp. 320–327
<b>Lesson 36</b>	<b>Partition Shapes to Make Equal Areas</b> —pp. 320–327

COMMON CORE STATE STANDARDS FOR MATHEMATICS, GRADE 3	
3.NF.1	Understand a fraction $1/b$ as the quantity formed by 1 part when a whole is partitioned into $b$ equal parts; understand a fraction $a/b$ as the quantity formed by $a$ parts of size $1/b$ .
3.G.2	Partition shapes into parts with equal areas. Express the area of each part as a unit fraction of the whole. <i>For example, partition a shape into 4 parts with equal area, and describe the area of each part as <math>1/4</math> of the area of the shape.</i>
3.G.2	Partition shapes into parts with equal areas. Express the area of each part as a unit fraction of the whole. <i>For example, partition a shape into 4 parts with equal area, and describe the area of each part as <math>1/4</math> of the area of the shape.</i>

<b>*12-1A</b>	<b>Use Fractions</b> —Online
---------------	------------------------------

<b>Lesson 36</b>	<b>Partition Shapes to Make Equal Areas</b> —pp. 320–327
------------------	--

3.G.2	Partition shapes into parts with equal areas. Express the area of each part as a unit fraction of the whole. <i>For example, partition a shape into 4 parts with equal area, and describe the area of each part as <math>1/4</math> of the area of the shape.</i>
-------	--

## Chapter 12 Fractions

PROGRESS IN MATHEMATICS, GRADE 3	COMMON CORE PROGRESS MATHEMATICS, GRADE 3	COMMON CORE STATE STANDARDS FOR MATHEMATICS, GRADE 3
<p><b>*12-1B Unit Fractions on a Number Line</b>—Online</p>	<p><b>Lesson 18 Understand Fractions on the Number Line</b>—pp. 158–165</p>	<p>3.NF.2a Represent a fraction <math>1/b</math> on a number line diagram by defining the interval from 0 to 1 as the whole and partitioning it into <math>b</math> equal parts. Recognize that each part has size <math>1/b</math> and that the endpoint of the part based at 0 locates the number <math>1/b</math> on the number line.</p> <p>3.NF.2b Represent a fraction <math>a/b</math> on a number line diagram by marking off a lengths <math>1/b</math> from 0. Recognize that the resulting interval has size <math>a/b</math> and that its endpoint locates the number <math>a/b</math> on the number line.</p>
<p><b>*12-1C Fractions on a Number Line</b>—Online</p>	<p><b>Lesson 16 Understand Unit Fractions as Quantities</b>—pp. 142–149</p> <p><b>Lesson 17 Understand Fractions as Quantities</b>—pp. 150–157</p> <p><b>Lesson 18 Understand Fractions on the Number Line</b>—pp. 158–165</p>	<p>3.NF.1 Understand a fraction <math>1/b</math> as the quantity formed by 1 part when a whole is partitioned into <math>b</math> equal parts; understand a fraction <math>a/b</math> as the quantity formed by <math>a</math> parts of size <math>1/b</math>.</p> <p>3.NF.2b Represent a fraction <math>a/b</math> on a number line diagram by marking off a lengths <math>1/b</math> from 0. Recognize that the resulting interval has size <math>a/b</math> and that its endpoint locates the number <math>a/b</math> on the number line.</p>
<p><b>12-2 Equivalent Fractions</b>—pp. 388–389</p>	<p><b>Lesson 19 Understand Equivalent Fractions</b>—pp. 166–173</p> <p><b>Lesson 20 Write Equivalent Fractions</b>—pp. 174–181</p>	<p>3.NF.3a Represent a fraction <math>1/b</math> on a number line diagram by defining the interval from 0 to 1 as the whole and partitioning it into <math>b</math> equal parts. Recognize that each part has size <math>1/b</math> and that the endpoint of the part based at 0 locates the number <math>1/b</math> on the number line.</p> <p>3.NF.3b Recognize and generate simple equivalent fractions, e.g., <math>1/2 = 2/4</math>, <math>4/6 = 2/3</math>). Explain why the fractions are equivalent, e.g., by using a visual fraction model.</p>

## Chapter 12 Fractions

## PROGRESS IN MATHEMATICS, GRADE 3

**\*12-2A Model Equivalent Fractions**—Online

**12-3 Estimate Fractions**—pp. 390–391

**\*12-3A Compare Like Fractions Using Models**—Online

## COMMON CORE PROGRESS MATHEMATICS, GRADE 3

**Lesson 22 Compare Fractions: Same Denominator**—  
pp. 190–197

**Lesson 23 Compare Fractions: Same Numerator**—  
pp. 198–205

**Lesson 19 Understand Equivalent Fractions**—pp.  
166–173

**Lesson 20 Write Equivalent Fractions**—pp. 174–181

**Lesson 21 Relate Whole Numbers and Fractions**—  
pp. 182–189

**Lesson 22 Compare Fractions: Same Denominator**—  
pp. 190–197

**Lesson 23 Compare Fractions: Same Numerator**—  
pp. 198–205

## COMMON CORE STATE STANDARDS FOR MATHEMATICS, GRADE 3

3.NF.3d Compare two fractions with the same numerator or the same denominator by reasoning about their size. Recognize that comparisons are valid only when the two fractions refer to the same whole. Record the results of comparisons with the symbols  $>$ ,  $=$ , or  $<$ , and justify the conclusions, e.g., by using a visual fraction model.

3.NF.3a Represent a fraction  $1/b$  on a number line diagram by defining the interval from 0 to 1 as the whole and partitioning it into  $b$  equal parts. Recognize that each part has size  $1/b$  and that the endpoint of the part based at 0 locates the number  $1/b$  on the number line.

3.NF.3b Recognize and generate simple equivalent fractions, e.g.,  $1/2 = 2/4$ ,  $4/6 = 2/3$ . Explain why the fractions are equivalent, e.g., by using a visual fraction model.

3.NF.3c Express whole numbers as fractions, and recognize fractions that are equivalent to whole numbers.

*Examples: Express 3 in the form  $3 = 3/1$ ; recognize that  $6/1 = 6$ ; locate  $4/4$  and 1 at the same point of a number line diagram.*

3.NF.3d Compare two fractions with the same numerator or the same denominator by reasoning about their size. Recognize that comparisons are valid only when the two fractions refer to the same whole. Record the results of comparisons with the symbols  $>$ ,  $=$ , or  $<$ , and justify the conclusions, e.g., by using a visual fraction model.

## Chapter 12 Fractions

## PROGRESS IN MATHEMATICS, GRADE 3

**12-4 Compare Fractions**—pp. 392–393

**\*12-4A Compare Unlike Fractions Using Fraction Strips**—Online

**\*12-4B Fraction Sense**—Online

**12-5 Order Fractions**—pp. 394–395

## COMMON CORE PROGRESS MATHEMATICS, GRADE 3

**Lesson 16 Understand Unit Fractions as Quantities**—pp. 142–149

**Lesson 17 Understand Fractions as Quantities**—pp. 150–157

**Lesson 18 Understand Fractions on the Number Line**—pp. 158–165

**Lesson 22 Compare Fractions: Same Denominator**—pp. 190–197

**Lesson 23 Compare Fractions: Same Numerator**—pp. 198–205

**Lesson 22 Compare Fractions: Same Denominator**—pp. 190–197

**Lesson 23 Compare Fractions: Same Numerator**—pp. 198–205

**Lesson 16 Understand Unit Fractions as Quantities**—pp. 142–149

**Lesson 17 Understand Fractions as Quantities**—pp. 150–157

## COMMON CORE STATE STANDARDS FOR MATHEMATICS, GRADE 3

3.NF.1 Understand a fraction  $1/b$  as the quantity formed by 1 part when a whole is partitioned into  $b$  equal parts; understand a fraction  $a/b$  as the quantity formed by  $a$  parts of size  $1/b$ .

3.NF.2a Represent a fraction  $1/b$  on a number line diagram by defining the interval from 0 to 1 as the whole and partitioning it into  $b$  equal parts. Recognize that each part has size  $1/b$  and that the endpoint of the part based at 0 locates the number  $1/b$  on the number line.

3.NF.2b Represent a fraction  $a/b$  on a number line diagram by marking off  $a$  lengths  $1/b$  from 0. Recognize that the resulting interval has size  $a/b$  and that its endpoint locates the number  $a/b$  on the number line.

3.NF.3d Compare two fractions with the same numerator or the same denominator by reasoning about their size. Recognize that comparisons are valid only when the two fractions refer to the same whole. Record the results of comparisons with the symbols  $>$ ,  $=$ , or  $<$ , and justify the conclusions, e.g., by using a visual fraction model.

3.NF.3d Compare two fractions with the same numerator or the same denominator by reasoning about their size. Recognize that comparisons are valid only when the two fractions refer to the same whole. Record the results of comparisons with the symbols  $>$ ,  $=$ , or  $<$ , and justify the conclusions, e.g., by using a visual fraction model.

3.NF.1 Understand a fraction  $1/b$  as the quantity formed by 1 part when a whole is partitioned into  $b$  equal parts; understand a fraction  $a/b$  as the quantity formed by  $a$  parts of size  $1/b$ .

## Chapter 12 Fractions

PROGRESS IN MATHEMATICS, GRADE 3	COMMON CORE PROGRESS MATHEMATICS, GRADE 3	COMMON CORE STATE STANDARDS FOR MATHEMATICS, GRADE 3
<b>12-6 Find Part of a Set</b> —pp. 396–397	<b>Lesson 22 Compare Fractions: Same Denominator</b> —pp. 190–197	<b>3.NF.3d</b> Compare two fractions with the same numerator or the same denominator by reasoning about their size. Recognize that comparisons are valid only when the two fractions refer to the same whole. Record the results of comparisons with the symbols $>$ , $=$ , or $<$ , and justify the conclusions, e.g., by using a visual fraction model.
<b>12-7 Mixed Numbers</b> —pp. 398–399	<b>Lesson 23 Compare Fractions: Same Numerator</b> —pp. 198–205	
<b>12-8 Add Fractions</b> —pp. 400–401	<b>Lesson 18 Understand Fractions on the Number Line</b> —pp. 158–165	<b>3.NF.2b</b> Represent a fraction $a/b$ on a number line diagram by marking off a lengths $1/b$ from 0. Recognize that the resulting interval has size $a/b$ and that its endpoint locates the number $a/b$ on the number line.
<b>12-9 Subtract Fractions</b> —pp. 402–403	<b>Lesson 20 Write Equivalent Fractions</b> —pp. 174–181	<b>3.NF.3b</b> Recognize and generate simple equivalent fractions, e.g., $1/2 = 2/4$ , $4/6 = 2/3$ . Explain why the fractions are equivalent, e.g., by using a visual fraction model.
<b>12-10 Unit Cost</b> —pp. 404–405		
<b>12-11 Problem Solving Strategy: Use a Drawing/Model</b> —pp. 406–407		
<b>12-12 Problem Solving Applications: Mixed Review</b> —pp. 408–409		

### Chapter 13 Decimals

PROGRESS IN MATHEMATICS, GRADE 3	
<b>13-1</b>	<b>Fractions and Decimals</b> —pp. 416–417
<b>13-2</b>	<b>Hundredths</b> —pp. 418–419
<b>13-3</b>	<b>Decimals Greater Than One</b> —pp. 420–421
<b>13-4</b>	<b>Compare and Order Decimals</b> —pp. 422–423
<b>13-5</b>	<b>Add and Subtract Decimals</b> —pp. 424–425
<b>13-6</b>	<b>Multiply Money</b> —pp. 426–427
<b>13-7</b>	<b>Divide Money</b> —pp. 428–429
<b>13-8</b>	<b>Problem Solving Strategy: Find a Pattern</b> —pp. 430–431
<b>13-9</b>	<b>Problem Solving Applications: Mixed Review</b> —pp. 432–433

COMMON CORE PROGRESS MATHEMATICS, GRADE 3	
<b>Lesson 12</b>	<b>Identify and Explain Arithmetic Patterns</b> —pp. 104–111

COMMON CORE STATE STANDARDS FOR MATHEMATICS, GRADE 3	
3.OA.9	Identify arithmetic patterns (including patterns in the addition table or multiplication table), and explain them using properties of operations.  <i>For example, observe that 4 times a number is always even, and explain why 4 times a number can be decomposed into two equal addends.</i>

### Chapter 14 Get Ready for Algebra

PROGRESS IN MATHEMATICS, GRADE 3	
<b>14-1</b>	<b>Divisibility</b> —pp. 440–441
<b>14-2</b>	<b>Expressions and Variables</b> —pp. 442–443

COMMON CORE PROGRESS MATHEMATICS, GRADE 3	
<b>Lesson 12</b>	<b>Identify and Explain Arithmetic Patterns</b> —pp. 104–111

COMMON CORE STATE STANDARDS FOR MATHEMATICS, GRADE 3	
3.OA.9	Identify arithmetic patterns (including patterns in the addition table or multiplication table), and explain them using properties of operations.  <i>For example, observe that 4 times a number is always even, and explain why 4 times a number can be decomposed into two equal addends.</i>

### Chapter 14 Get Ready for Algebra

PROGRESS IN MATHEMATICS, GRADE 3

\*14-2A **Writing Variable Equations**—Online

14-3 **Order of Operations**—pp. 444–445

14-4 **Missing Operation**—pp. 446–447

14-5 **Factors**—pp. 448–449

14-6 **Number Sentences**—pp. 450–451

14-7 **Problem Solving Strategy: Use More Than One Step**—pp. 452–453

COMMON CORE PROGRESS MATHEMATICS, GRADE 3

**Lesson 10 Problem Solving: Two-Step Problems**—pp. 88–95

**Lesson 11 Problem Solving: Use Equations**—pp. 96–103

**Lesson 10 Problem Solving: Two-Step Problems**—pp. 88–95

**Lesson 11 Problem Solving: Use Equations**—pp. 96–103

**Lesson 33 Problem Solving: Perimeter**—pp. 296–303

**Lesson 34 Problem Solving: Compare Perimeter and Area**—pp. 304–311

COMMON CORE STATE STANDARDS FOR MATHEMATICS, GRADE 3

3.OA.8 Solve two-step word problems using the four operations. Represent these problems using equations with a letter standing for the unknown quantity. Assess the reasonableness of answers using mental computation and estimation strategies including rounding.<sup>3</sup>

<sup>3</sup>This standard is limited to problems posed with whole numbers and having whole-number answers; students should know how to perform operations in the conventional order when there are no parentheses to specify a particular order (Order of Operations).

3.OA.8 Solve two-step word problems using the four operations. Represent these problems using equations with a letter standing for the unknown quantity. Assess the reasonableness of answers using mental computation and estimation strategies including rounding.<sup>3</sup>

<sup>3</sup>This standard is limited to problems posed with whole numbers and having whole-number answers; students should know how to perform operations in the conventional order when there are no parentheses to specify a particular order (Order of Operations).

3.MD.8 Solve real world and mathematical problems involving perimeters of polygons, including finding the perimeter given the side lengths, finding an unknown side length, and exhibiting rectangles with the same perimeter and different areas or with the same area and different perimeters.

## Chapter 14 Get Ready for Algebra

## PROGRESS IN MATHEMATICS, GRADE 3

**14-8 Problem Solving Applications: Mixed Review**—pp. 454–455

## COMMON CORE PROGRESS MATHEMATICS, GRADE 3

**Lesson 10 Problem Solving: Two-Step Problems**—pp. 88–95

**Lesson 11 Problem Solving: Use Equations**—pp. 96–103

## COMMON CORE STATE STANDARDS FOR MATHEMATICS, GRADE 3

3.OA.8 Solve two-step word problems using the four operations. Represent these problems using equations with a letter standing for the unknown quantity. Assess the reasonableness of answers using mental computation and estimation strategies including rounding.<sup>3</sup>

<sup>3</sup>This standard is limited to problems posed with whole numbers and having whole-number answers; students should know how to perform operations in the conventional order when there are no parentheses to specify a particular order (Order of Operations).