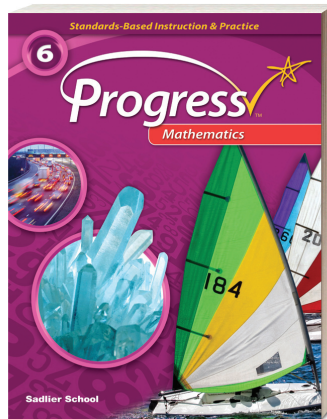SADLIER

Progress
Mathematics
Standards-Based Instruction & Practice

Aligned to

Tennessee's State Mathematics Standards

Grade 6

Contents

Ratios and Proportional Relationships

CLUSTER / STANDARD	SADLIER *PROGRESS MATHEMATICS*, GRADE 6
Understand ratio concepts and use ratio reasoning to solve problems.	
1. Understand the concept of a ratio and use ratio language to describe a ratio relationship between two quantities. *For example, "The ratio of wings to beaks in the bird house at the zoo was 2:1, because for every 2 wings there was 1 beak." "For every vote candidate A received, candidate C received nearly three votes."*	**Lesson 1** **Understand Ratios and Unit Rates**—pp. 10–17
2. Understand the concept of a unit rate a/b associated with a ratio $a{:}b$ with $b \neq 0$, and use rate language in the context of a ratio relationship. *For example, "This recipe has a ratio of 3 cups of flour to 4 cups of sugar, so there is 3/4 cup of flour for each cup of sugar." "We paid $75 for 15 hamburgers, which is a rate of $5 per hamburger."* (Expectations for unit rates in this grade are limited to non-complex fractions.)	**Lesson 1** **Understand Ratios and Unit Rates**—pp. 10–17
3. Use ratio and rate reasoning to solve real-world and mathematical problems, e.g., by reasoning about tables of equivalent ratios, tape diagrams, double number line diagrams, or equations.	**Lesson 8** **Problem Solving: Ratios and Rates**—pp. 66–73
a. Make tables of equivalent ratios relating quantities with whole-number measurements, find missing values in the tables, and plot the pairs of values on the coordinate plane. Use tables to compare ratios.	**Lesson 2** **Use Ratio Tables to Find Equivalent Ratios**—pp. 18–25 **Lesson 3** **Use Ratio Tables to Compare Ratios**—pp. 26–33
b. Solve unit rate problems including those involving unit pricing and constant speed. *For example, if it took 7 hours to mow 4 lawns, then at that rate, how many lawns could be mowed in 35 hours? At what rate were lawns being mowed?*	**Lesson 4** **Solve Unit Rate Problems**—pp. 34–41
c. Find a percent of a quantity as a rate per 100 (e.g., 30% of a quantity means 30/100 times the quantity); solve problems involving finding the whole, given a part and the percent.	**Lesson 5** **Calculate a Percent of a Quantity**—pp. 42–49 **Lesson 6** **Find the Whole Given a Part and the Percent**—pp. 50–57
d. Use ratio reasoning to convert measurement units; manipulate and transform units appropriately when multiplying or dividing quantities.	**Lesson 7** **Convert Measurement Units**—pp. 58–65

The Number System

CLUSTER / STANDARD	SADLIER *PROGRESS MATHEMATICS*, GRADE 6
Apply and extend previous understandings of multiplication and division to divide fractions by fractions.	
1. Interpret and compute quotients of fractions, and solve word problems involving division of fractions by fractions, e.g., by using visual fraction models and equations to represent the problem. *For example, create a story context for (2/3) ÷ (3/4) and use a visual fraction model to show the quotient; use the relationship between multiplication and division to explain that (2/3) ÷ (3/4) = 8/9 because 3/4 of 8/9 is 2/3. (In general, (a/b) ÷ (c/d) = ad/bc.) How much chocolate will each person get if 3 people share 1/2 lb of chocolate equally? How many 3/4-cup servings are in 2/3 of a cup of yogurt? How wide is a rectangular strip of land with length 3/4 mi and area 1/2 square mi?*	**Lesson 9** **Divide a Fraction by a Fraction**—pp. 80–87 **Lesson 10** **Problem Solving: Fraction Division**—pp. 88–95
Compute fluently with multi-digit numbers and find common factors and multiples.	
2. Fluently divide multi-digit numbers using the standard algorithm.	**Lesson 11** **Divide Multi-digit Numbers**—pp. 96–103
3. Fluently add, subtract, multiply, and divide multi-digit decimals using the standard algorithm for each operation.	**Lesson 12** **Add and Subtract Multi-digit Decimals**—pp. 104–111 **Lesson 13** **Multiply and Divide Multi-digit Decimals**—pp. 112–119
4. Find the greatest common factor of two whole numbers less than or equal to 100 and the least common multiple of two whole numbers less than or equal to 12. Use the distributive property to express a sum of two whole numbers 1–100 with a common factor as a multiple of a sum of two whole numbers with no common factor. *For example, express 36 + 8 as 4 (9 + 2).*	**Lesson 14** **Find the Greatest Common Factor and Least Common Multiple**—pp. 120–127
Apply and extend previous understandings of numbers to the system of rational numbers.	
5. Understand that positive and negative numbers are used together to describe quantities having opposite directions or values (e.g., temperature above/below zero, elevation above/below sea level, credits/debits, positive/negative electric charge); use positive and negative numbers to represent quantities in real-world contexts, explaining the meaning of 0 in each situation.	**Lesson 15** **Understand Positive and Negative Numbers and Opposites**—pp. 128–135

The Number System

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6. Understand a rational number as a point on the number line. Extend number line diagrams and coordinate axes familiar from previous grades to represent points on the line and in the plane with negative number coordinates.	
a. Recognize opposite signs of numbers as indicating locations on opposite sides of 0 on the number line; recognize that the opposite of the opposite of a number is the number itself, e.g., –(–3) = 3, and that 0 is its own opposite.	**Lesson 15** **Understand Positive and Negative Numbers and Opposites**—pp. 128–135
b. Understand signs of numbers in ordered pairs as indicating locations in quadrants of the coordinate plane; recognize that when two ordered pairs differ only by signs, the locations of the points are related by reflections both axes.	**Lesson 16** **Locate Points with Rational Coordinates**—pp. 136–143
c. Find and position integers and other rational numbers on a horizontal or vertical number line diagram; find and position pairs of integers and other rational numbers on a coordinate plane.	**Lesson 16** **Locate Points with Rational Coordinates**—pp. 136–143
7. Understand ordering and absolute value of rational numbers.	
a. Interpret statements of inequality as statements about the relative position of two numbers on a number line diagram. *For example, interpret –3 > –7 as a statement that –3 is located to the right of –7 on a number line oriented from left to right.*	**Lesson 17** **Compare and Order Rational Numbers**—pp. 144–151
b. Write, interpret, and explain statements of order for rational numbers in real-world contexts. *For example, write –3° C > –7° C to express the fact that –3° C is warmer than –7° C.*	**Lesson 17** **Compare and Order Rational Numbers**—pp. 144–151
c. Understand the absolute value of a rational number as its distance from 0 on the number line; interpret absolute value as magnitude for a positive or negative quantity in a real-world situation. *For example, for an account balance of –30 dollars, write |–30| = 30 to describe the size of the debt in dollars.*	**Lesson 18** **Understand Absolute Value**—pp. 152–159
d. Distinguish comparisons of absolute value from statements about order. *For example, recognize that an account balance less than –30 dollars represents a debt greater than 30 dollars.*	**Lesson 18** **Understand Absolute Value**—pp. 152–159

The Number System

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8. Solve real-world and mathematical problems by graphing points in all four quadrants of the coordinate plane. Include use of coordinates and absolute value to find distances between points with the same first coordinate or the same second coordinate.	**Lesson 19** **Problem Solving: The Coordinate Plane**—pp. 160–167

Expressions and Equations

Cluster / Standard	Sadlier *Progress Mathematics*, Grade 6
Apply and extend previous understandings of arithmetic to algebraic expressions.	
1. Write and evaluate numerical expressions involving whole-number exponents.	**Lesson 20** **Write and Evaluate Numerical Expressions with Exponents** —pp. 174–181
2. Write, read, and evaluate expressions in which letters stand for numbers.	
a. Write expressions that record operations with numbers and with letters standing for numbers. *For example, express the calculation "Subtract y from 5" as 5 – y.*	**Lesson 21** **Write Algebraic Expressions to Record Operations**—pp. 182–189
b. Identify parts of an expression using mathematical terms (sum, term, product, factor, quotient, coefficient); view one or more parts of an expression as a single entity. F*or example, describe the expression 2 (8 + 7) as a product of two factors; view (8 + 7) as both a single entity and a sum of two terms.*	**Lesson 22** **Identify Parts of an Expression**—pp. 190–197
c. Evaluate expressions at specific values of their variables. Include expressions that arise from formulas used in real-world problems. Perform arithmetic operations, including those involving whole-number exponents, in the conventional order when there are no parentheses to specify a particular order (Order of Operations). *For example, use the formulas $V = s^3$ and $A = 6 s^2$ to find the volume and surface area of a cube with sides of length s = 1/2.*	**Lesson 23** **Evaluate Algebraic Expressions**—pp. 198–205
3. Apply the properties of operations to generate equivalent expressions. *For example, apply the distributive property to the expression 3 (2 + x) to produce the equivalent expression 6 + 3x; apply the distributive property to the expression 24x + 18y to produce the equivalent expression 6 (4x + 3y); apply properties of operations to y + y + y to produce the equivalent expression 3y.*	**Lesson 24** **Generate and Identify Equivalent Expressions**—pp. 206–213

Expressions and Equations

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4. Identify when two expressions are equivalent (i.e., when the two expressions name the same number regardless of which value is substituted into them). *For example, the expressions y + y + y and 3y are equivalent because they name the same number regardless of which number y stands for.*	**Lesson 24** **Generate and Identify Equivalent Expressions**—pp. 206–213

Reason about and solve one-variable equations and inequalities.

5. Understand solving an equation or inequality as a process of answering a question: which values from a specified set, if any, make the equation or inequality true? Use substitution to determine whether a given number in a specified set makes an equation or inequality true.	**Lesson 25** **Identify Solutions to Equations and Inequalities**—pp. 214–221
6. Use variables to represent numbers and write expressions when solving a real-world or mathematical problem; understand that a variable can represent an unknown number, or, depending on the purpose at hand, any number in a specified set.	**Lesson 26** **Write Algebraic Expressions to Represent Problems**—pp. 222–229
7. Solve real-world and mathematical problems by writing and solving equations of the form $x + p = q$ and $px = q$ for cases in which p, q and x are all nonnegative rational numbers.	**Lesson 27** **Solve Equations of the Form x + p = q**—pp. 230–237
	Lesson 28 **Solve Equations of the Form px = q**—pp. 238–245
8. Write an inequality of the form $x > c$ or $x < c$ to represent a constraint or condition in a real-world or mathematical problem. Recognize that inequalities of the form $x > c$ or $x < c$ have infinitely many solutions; represent solutions of such inequalities on number line diagrams.	**Lesson 29** **Graph Solutions to Inequalities**—pp. 246–253

Represent and analyze quantitative relationships between dependent and independent variables.

9. Use variables to represent two quantities in a real-world problem that change in relationship to one another; write an equation to express one quantity, thought of as the dependent variable, in terms of the other quantity, thought of as the independent variable. Analyze the relationship between the dependent and independent variables using graphs and tables, and relate these to the equation. *For example, in a problem involving motion at constant speed, list and graph ordered pairs of distances and times, and write the equation d = 65t to represent the relationship between distance and time.*	**Lesson 30** **Represent Relationships Between Variables**—pp. 254–261

Geometry

CLUSTER / STANDARD	SADLIER *PROGRESS MATHEMATICS*, GRADE 6
Solve real-world and mathematical problems involving area, surface area, and volume.	
1. Find the area of right triangles, other triangles, special quadrilaterals, and polygons by composing into rectangles or decomposing into triangles and other shapes; apply these techniques in the context of solving real-world and mathematical problems.	**Lesson 31** **Find Areas of Parallelograms and Triangles**—pp. 268–275
	Lesson 32 **Find Areas of Polygons**—pp. 276–283
2. Find the volume of a right rectangular prism with fractional edge lengths by packing it with unit cubes of the appropriate unit fraction edge lengths, and show that the volume is the same as would be found by multiplying the edge lengths of the prism. Apply the formulas $V = l\,w\,h$ and $V = b\,h$ to find volumes of right rectangular prisms with fractional edge lengths in the context of solving real-world and mathematical problems.	**Lesson 33** **Find Volumes of Rectangular Prisms**—pp. 284–291
3. Draw polygons in the coordinate plane given coordinates for the vertices; use coordinates to find the length of a side joining points with the same first coordinate or the same second coordinate. Apply these techniques in the context of solving real-world and mathematical problems.	**Lesson 34** **Plot and Analyze Polygons in the Coordinate Plane**—pp. 292–299
4. Represent three-dimensional figures using nets made up of rectangles and triangles, and use the nets to find the surface area of these figures. Apply these techniques in the context of solving real-world and mathematical problems.	**Lesson 35** **Use Nets to Find Surface Area**—pp. 300–307

Statistics and Probability

CLUSTER / STANDARD	SADLIER *PROGRESS MATHEMATICS*, GRADE 6
Develop understanding of statistical variability.	
1. Recognize a statistical question as one that anticipates variability in the data related to the question and accounts for it in the answers. *For example, "How old am I?" is not a statistical question, but "How old are the students in my school?" is a statistical question because one anticipates variability in students' ages.*	**Lesson 36** **Understand Statistical Questions and Describe Data**—pp. 314–321
2. Understand that a set of data collected to answer a statistical question has a distribution which can be described by its center, spread, and overall shape.	**Lesson 36** **Understand Statistical Questions and Describe Data**—pp. 314–321
	Lesson 37 **Find the Median and Interquartile Range**—pp. 322–329

Statistics and Probability

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3. Recognize that a measure of center for a numerical data set summarizes all of its values with a single number, while a measure of variation describes how its values vary with a single number.	**Lesson 37** **Find the Median and Interquartile Range**—pp. 322–329
	Lesson 38 **Find the Mean and Mean Absolute Deviation**—pp. 330–337

Summarize and describe distributions.

4. Display numerical data in plots on a number line, including dot plots, histograms, and box plots.	**Lesson 39** **Display Numerical Data**—pp. 338–345
5. Summarize numerical data sets in relation to their context, such as by:	
a. Reporting the number of observations.	**Lesson 40** **Summarize Numerical Data**—pp. 346–353
b. Describing the nature of the attribute under investigation, including how it was measured and its units of measurement.	**Lesson 40** **Summarize Numerical Data**—pp. 346–353
c. Giving quantitative measures of center (median and/or mean) and variability (interquartile range and/or mean absolute deviation), as well as describing any overall pattern and any striking deviations from the overall pattern with reference to the context in which the data were gathered.	**Lesson 40** **Summarize Numerical Data**—pp. 346–353
d. Relating the choice of measures of center and variability to the shape of the data distribution and the context in which the data were gathered.	**Lesson 40** **Summarize Numerical Data**—pp. 346–353